Rauli Susmel Econometrics 1

## Homework 2

1. Suppose **b** is the least squares coefficient vector in the regression of **y** on **X** and **c** is any other Kx1 vector. Prove that the difference in the two sums of squared residuals is (y-Xc)'(y-Xc) - (y-Xb)'(y-Xb) = (c - b)'X'X(c - b). Prove that this difference is positive.

2. Consider the least squares regression of y on K variables (with a constant), X. Consider an alternative set of regressors, Z = X+P, where P is a nonsingular non-random matrix. Calculate the residual vectors in the regressions of y on X and y on Z. What can you say about them?. What relevance does this have to the question of changing the fit of a regression by adding a constant to the measurement of the independent variables?

3. In the least squares regression of y on a constant and X, in order to compute the regression coefficients on X, we can first transform y to deviations from the mean, y, and, likewise, transform each column of X to deviations from the respective column means; second, regress the transformed y on the transformed X without a constant. Do we get the same result if we only transform y? What if we only transform X?

**4.** Prove that the adjusted  $R^2$  rises (falls) when variable  $\mathbf{x}_k$  is deleted from the regression if the square of the t ratio on  $\mathbf{x}_k$  in the multiple regression is less (greater) than one.

5. Suppose you estimate a multiple regression first with then without a constant. Whether the R<sup>2</sup> is higher in the second case than the first will depend in part on how it is computed. Using the (relatively) standard method,  $R^2 = 1 - e'e / y'M^0y$ , which regression will have a higher R<sup>2</sup>?

6. (Download dataset ec1\_set1.xlsx from website). You have monthly data on Disney stock returns,  $DIS\_ret$ , S&P 500 index returns, percent changes in the Fed's Broad Dollar Index,  $FR\_FXB$ , and the FF factors:  $Mkt\_RF$ , SMB, HML, and the risk free rate, RF. The data covers the period 1973:Jan to 2019:June. First, you transform Disney's returns into excess returns, that is,  $DIS\_er = DIS\_ret - RF$ . You fit the following regressions (with a constant):

- Reg 1: a regression of DIS er on Mkt-RF.

- Reg 2: a regression of *DIS\_er* on *Mkt-RF*, *SMB*, *HML*, and *FR\_FXB*.
- (a) Explain why specification (Reg 1) is a restricted version of specification (Reg 3), stating and interpreting the restriction.
- (b) Perform an *F* test of the restriction. Perform a *t* test of the restriction. Explain whether the *F* test and the *t* test could lead to different conclusions.

- (c) Supposing the restriction to be valid, explain whether you expect the coefficient of *Mkt-RF* and its standard error to differ, or be similar, in specifications (Reg 1) and (Reg 2).
- (d) Supposing the restriction to be invalid, how would you expect the coefficient of *Mkt*-*RF* and its standard error to differ, or be similar, in specifications (Reg 1) and (Reg 2)?
- (e) At a seminar, a commentator says that DIS has transformed itself, since 1993, embarking on an acquisition spree (Miramax, Capital Cities/ABC/ESPN, Fox Family, The Muppets, Pixar, Marvel, Lucasfilm, 21<sup>st</sup> Century Fox, etc.). Test whether the commentator's assertion is correct.
- (f) What are the implications of the commentator's assertion for the test of the above restriction?