

HEDGING FX RISK

Measuring and Managing FX Exposure

(for private use, not to be posted/shared online)

- **Last Class**

- **Hedging Market-based Tools:**

- ◆ **Futures/Forward:** Completely eliminates uncertainty

- ◇ UP: *short* in the foreign currency.

- HP: **long** in currency futures.

- ◇ UP: *long* in the foreign currency.

- HP: **short** in currency futures.

- ◆ **Options:** Reduces uncertainty. How much? It depends on **X**.

- ◇ UP: *short* in the foreign currency.

- HP: **long** in currency **calls**.

- ◇ UP: *long* in the foreign currency.

- HP: **long** in currency **puts**.

- **This Class**

- **Exposure (Risk)**

- At the firm level, currency risk is called *exposure*.

- **Three areas**

(1) *Transaction exposure*: Risk of transactions denominated in FC with a payment date or maturity.

(2) *Economic exposure*: Degree to which a firm's expected cash flows are affected by unexpected changes in S_t .

(3) *Translation exposure*: Accounting-based changes in a firm's consolidated statements that result from a change in S_t . Translation rules create accounting gains/losses due to changes in S_t .

We say a firm is “*exposed*” or *has exposure* if it faces currency risk.

- **This Class**

Example: Exposure.

A. *Transaction exposure*.

Swiss Cruises, a Swiss firm, sells cruise packages priced in USD to a broker. Payment in 30 days.

B. *Economic exposure*.

Swiss Cruises has 50% of its revenue denominated in USD and only 20% of its cost denominated in USD. A depreciation of the USD will affect future CHF cash flows.

C. *Translation exposure*.

Swiss Cruises obtains a USD loan from a U.S. bank. This liability has to be translated into CHF following Swiss accounting rules. ¶

- **This Class**

Q: How can FX changes affect the firm?

- *Transaction Exposure*

- Short-term CFs: Existing contract obligations.

- *Economic Exposure*

- Future CFs: Erosion of competitive position.

- *Translation Exposure*

- Revaluation of balance sheet (Book Value vs Market Value).

- **This Class**

- Measuring TE:

- $TE_{j,t} = \text{Value of a fixed future transaction in FC}_j * S_t$

- Netting TE (portfolio approach) = $NTE = \sum_{j=1}^J TE_{j,t}$

Remark: The risk in TE is driven by S_t

$\Rightarrow \Delta TE = TE_{t+T} - TE_t = \text{Value of a fixed future transaction in FC} * \Delta S$

- Range for TE:

- (1) Ad-hoc rule (say, $\pm 10\%$)

- (2) Sensitivity Analysis (Simulating exchange rates).

- (3) Assuming a statistical distribution for exchange rates.

- VaR: Worst case scenario in a given time interval within a (one-sided) CI.

- Lower-end of Receivables.

- Highest-end of Payables.

- **This Class**

- Measuring EE:

- Change in CF due to an *unexpected* change in S_t .

$$= \frac{\Delta CF_t}{\Delta S_t} \quad (\text{differential or derivative, } \Delta S_t \text{ is small})$$

- ΔCF_t can be approximated by change in Stock Prices.

Remark: If a company is publicly traded, ΔCF_t can be approximated by change in Stock Prices ΔP_t . A regression can be used.

Measuring Transaction Exposure

- Transaction exposure (TE) is easy to identify and measure.

- Identification: Transactions denominated in FC with a **fixed** future date

- Measure: Translate identified FC transactions to DC using S_t .

$$TE_{j,t} = \text{Value of a fixed future transaction in FC}_j * S_t$$

Example: Swiss Cruises.

Sold cruise packages for USD 2.5 million. Payment: 30 days.

Bought fuel oil for USD 1.5 million. Payment: 30 days.

$S_t = 1.45 \text{ CHF/USD}$.

Thus, the net transaction exposure in USD 30 days is:

$$\begin{aligned} \text{Net } TE_{j=USD} &= (\text{USD } 2.5\text{M} - \text{USD } 1.5\text{M}) * 1.45 \text{ CHF/USD} \\ &= \text{USD } 1\text{M} * 1.45 \text{ CHF/USD} = \text{CHF } 1.45\text{M}. \quad \blacksquare \end{aligned}$$

- **Netting**

An MNC has many transactions, in different currencies, with fixed futures dates. Since TE is denominated in DC, all exposures are easy to consolidate in one single number: Net TE (NTE).

$$\text{NTE} = \text{Net } TE_t = \sum_{j=1}^J TE_{j,t} \quad j = \text{EUR, GBP, JPY, BRL, MXN, ...}$$

- NTE is reported by fixed date: up to 90 days, more than 90-days, etc.

Note: Since currencies are correlated, firms take into account **correlations** to calculate how changes in S_t affect Net TE \Rightarrow **Portfolio Approach**.

Example: A U.S. MNC: Subsidiary A with CF(in EUR) > 0
 Subsidiary B with CF(in GBP) < 0

Since $\rho_{\text{GBP, EUR}}$ is very high and positive, NTE may be very low. ¶

\Rightarrow Hedging decisions are usually made based on exposure of the **portfolio**.

- **Netting - Correlations**

Example: Swiss Cruises.

Net Inflows (in USD): **USD 1 million**. Due: 30 days.

Loan repayment: **CAD 1.50 million**. Due: 30 days.

$S_t = 1.47 \text{ CAD/USD}$.

$\rho_{\text{CAD, USD}} = .843$ (monthly from 1971 to 2017)

Swiss Cruises considers NTE to be close to zero. ¶

Note 1: Correlations vary a lot across currencies. In general, **regional** currencies are highly correlated.

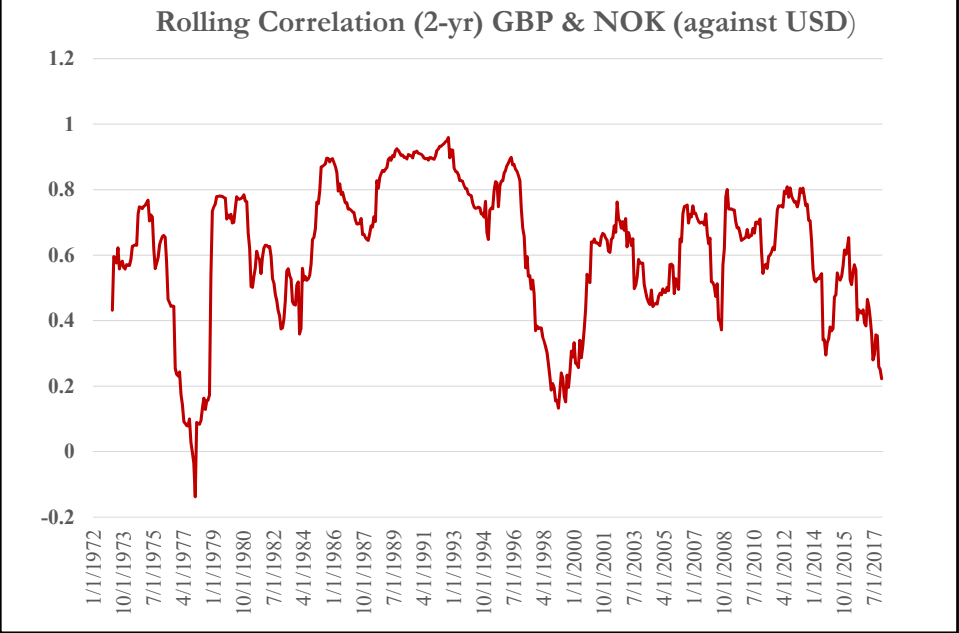
From **2000-2017**,

$$\rho_{\text{GBP, NOK}} = \mathbf{0.58}$$

$$\rho_{\text{GBP, JPY}} = \mathbf{0.04}$$

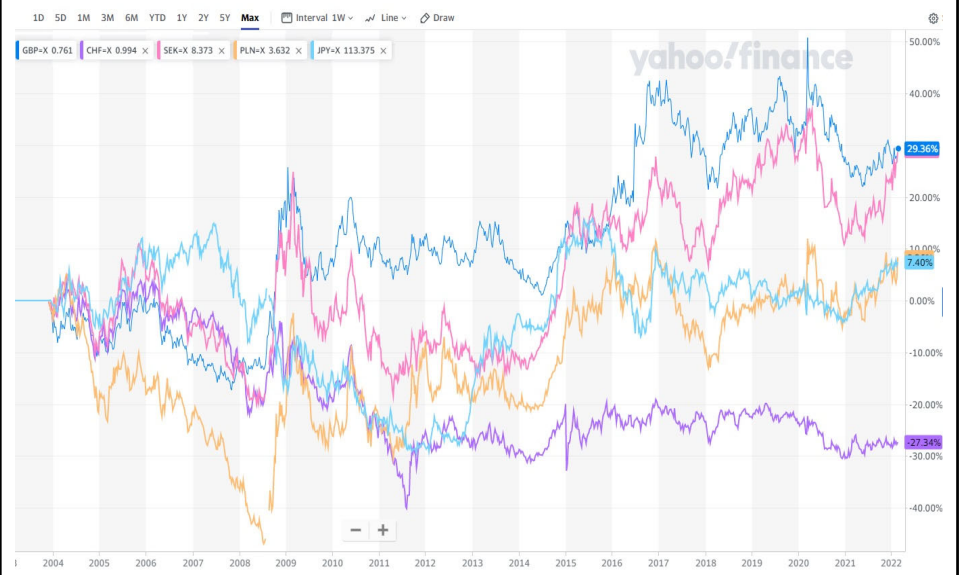
Note 2: Correlations also vary over time.

• Netting - Correlations



• Netting - Correlations

On average, currencies from developed countries tend to move together...
But, not all and not always.



• **Q: How does TE affect a firm in the future?**

Firms are interested in how TE will change in the future, say, in T days when transaction will be settled.

- Firms do not know S_{t+T} , they need to forecast $S_{t+T} \Rightarrow E_t[S_{t+T}]$

- Once we forecast $E_t[S_{t+T}]$, we can forecast $E_t[TE_{t+T}]$:

$$E_t[TE_{t+T}] = \text{Value of a fixed future transaction in FC} * E_t[S_{t+T}]$$

- $E_t[S_{t+T}]$ has an associated standard error, which can be used to create a range (or interval) for S_{t+T} & TE.

- Risk management perspective:

How much DC can the firm spend on account of a FC inflow in T days?

How much DC will be needed to cover a FC outflow in T days?.

Range Estimates of TE

• S_t is very difficult to forecast. Thus, a range estimate for NTE provides a useful number for risk managers.

The smaller the range, the lower the sensitivity of NTE.

• Three popular methods for estimating a range for NTE:

- (1) Ad-hoc rule (say, $\pm 10\%$)
- (2) Sensitivity Analysis (or simulating exchange rates)
- (3) Assuming a statistical distribution for exchange rates.

- **Ad-hoc Rule**

Many firms use an *ad-hoc* (“arbitrary”) rule to get a range: $\pm X\%$ (for example, a **10% rule**)

Simple and easy to understand: Get TE and add/subtract $\pm X\%$.

Example: 10% Rule.

SC has a Net TE = **CHF 1.45M** due in 30 days

⇒ if S_t changes by $\pm 10\%$, NTE changes by \pm **CHF 145,000**. ¶

Note: This example gives a range for NTE:

$$\text{NTE} \in [\text{CHF 1.305M}; \text{CHF 1.595M}]$$

Risk Management Interpretation: A risk manager will only care about the lower bound. If SC is counting on the **USD 1M** inflow to pay CHF expenses, these expenses should not exceed **CHF 1.305M**. ¶

- **Sensitivity Analysis**

Goal: Measure the sensitivity of TE to different exchange rates.

Example: Sensitivity of TE to extreme forecasts of S_t .

Sensitivity of TE to randomly simulate thousands of S_t .

Data: 20 years of monthly CHF/USD % changes (ED)

Mean (μ)	-0.00152	$\mu_m = -0.152\%$
Standard Error	0.00202	
Median	-0.00363	
Mode	#N/A	
Stand Deviation (σ)	0.03184	$\sigma_m = 3.184\%$
Sample Variance (σ^2)	0.00101	
Kurtosis	0.46327	
Skewness	0.42987	
Range	0.27710	
Minimum	-0.11618	
Maximum	0.15092	
Sum	0.0576765	
Count	248	

• **Sensitivity Analysis – Extremes (Worst Case & Best Case)**

Example: Extremes for Swiss Cruises Net TE (CHF/USD)

ED of S_t monthly changes over the past 20 years (1994-2014).

Extremes: **15.09%** (on October 2011) and **-11.62%** (on Jan 2009).

SC's net receivables in FC: **USD 1M**.

(A) *Best case scenario*: largest appreciation of USD: **0.1509**

NTE: **USD 1M** * **1.45 CHF/USD** * (1 + **0.1509**) = **CHF 1,668,805**.

(B) *Worst case scenario*: largest depreciation of USD: **-0.1162**

NTE: **USD 1M** * **1.45 CHF/USD** * (1 + (**-0.1162**)) = **CHF 1,281,510**.

That is,

$$\text{NTE} \in [\text{CHF } 1,281,510; \text{CHF } 1,668,805]$$

Note: If Swiss Cruises is counting on the USD 1M to cover CHF expenses, the expenses to cover should not exceed **CHF 1,281,510**. ¶

• **Sensitivity Analysis – Simulation**

Managers may consider the previous range, based on extremes, too conservative:

$$\text{NTE} \in [\text{CHF } 1,281,510; \text{CHF } 1,668,805].$$

⇒ Probability of worst case scenario is low: Only once in 240 months!

Under more likely scenarios, a firm may be able to cover more expenses.

A more realistic range can be constructed through sampling from the ED.

Example: Simulation for SC's Net TE (CHF/USD) over one month.

(i) Randomly pick 1,000 monthly s_{t+30} 's from the ED.

(ii) Calculate S_{t+30} for each s_{t+30} selected in (i).

$$\text{(Recall: } S_{t+30} = 1.45 \text{ CHF/USD} * (1 + s_{t+30}))$$

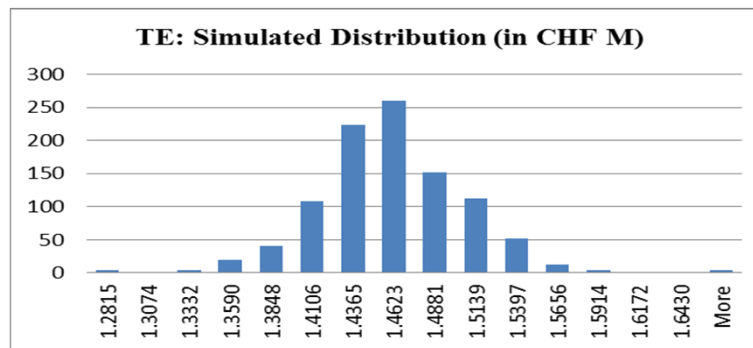
(iii) Calculate **TE** for each S_{t+30} . (Recall: **TE** = **USD 1M** * S_{t+30})

(iv) Plot the 1,000 **TE**'s in a histogram. (Simulated TE distribution.)

Example (continuation): In excel, using Vlookup function

- (i) Randomly draw $s_t = s_{sim,1}$ from ED: Observation 19: $s_{t+30} = 0.0034$.
(ii) Calculate $S_{sim,1}$: $S_{t+30} = 1.45 \text{ CHF/USD} * (1 + .0034) = 1.4549$
(iii) Calculate $TE_{sim,1}$: $TE = \text{USD } 1\text{M} * S_{t+30} = 1,454,937.57$
(iv) Repeat (i)-(iii) 1,000 times. Plot histogram. Construct a $(1-\alpha)\%$ C.I.

Lookup cell	Random Draw		Draw s_{sim}		TE(sim)
	s_t	with Randbetween	with Vlookup	S_{sim}	
1					
2	0.0025	19	0.0034	1.4549	1,454,937.57
3	-0.0027	147	-0.0104	1.4349	1,434,895.83
4	0.0001	99	0.0125	1.4682	1,468,189.96
5	-0.0443	203	-0.0584	1.3653	1,365,272.92
6	-0.0017	82	-0.0727	1.3446	1,344,597.25
7	-0.0031	4	0.0001	1.4502	1,450,168.79
8	-0.0227	67	-0.0226	1.4172	1,417,218.22
9	-0.0099	136	0.0095	1.4638	1,463,838.02
10	0.0098	232	0.0191	1.4777	1,477,749.46



Based on this simulated distribution, we can estimate a 95% range (leaving 2.5% observations to the left and 2.5% observations to the right)

$$\Rightarrow \text{NTE} \in [\text{CHF } 1.3661 \text{ M}; \text{CHF } 1.5443 \text{ M}]$$

Practical Application: If SC expects to cover expenses with this USD inflow, the maximum amount in CHF to cover, using this 95% CI, should be **CHF 1,366,100.** ¶

- **Aside: How many draws in the simulations?**

Usually, we draw until the CIs do not change a lot.

Example: 1,000 and 10,000 draws

For the SC example, we drew **1,000** scenarios to get a 95% C.I.:

$$\Rightarrow \text{NTE} \in [\text{CHF } 1.3661 \text{ M}; \text{ CHF } 1.5443 \text{ M}]$$

Now, we draw **10,000** scenarios and determined the following 95% C.I.:

$$\Rightarrow \text{NTE} \in [\text{CHF } 1.3670 \text{ M}; \text{ CHF } 1.5446 \text{ M}]$$

- Not a significant change in the range: 1,000 simulations seem enough.

- **Assuming a Distribution**

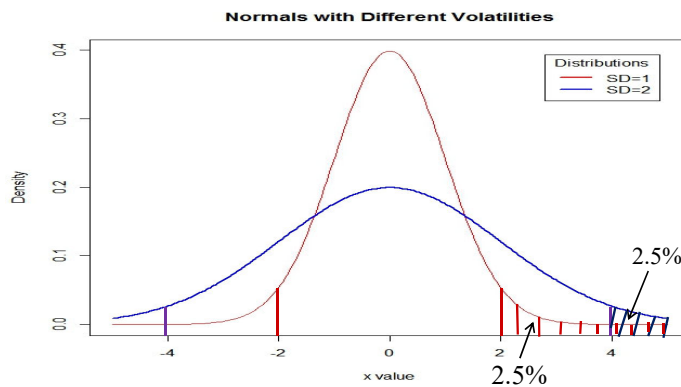
CIs based on an assumed distribution provide a range for TE.

For example, a firm assumes that $s_t \sim N(\mu, \sigma^2)$. (“ \sim ” = follows)

$$\Rightarrow \text{construct a } (1-\alpha)\% \text{ CI: } [\mu \pm z_{\alpha/2} \sigma].$$

Usual α 's: $\alpha = .05$ $\Rightarrow z_{.025} = 1.96 (\approx 2)$

$\alpha = .02$ $\Rightarrow z_{.01} = 2.33$



• **Assuming a Distribution – Normal for s_t**

Example: CI range based on a Normal distribution.

Swiss Cruises believes that CHF/USD monthly changes follow a normal distribution. SC estimates:

μ = Monthly mean = **-0.00152** \approx -0.15%

σ^2 = Monthly variance = 0.001014 ($\Rightarrow \sigma =$ **0.03184**, or 3.18%)

$s_t \sim N(-0.00152, 0.03184^2)$ s_t = CHF/USD monthly changes.

SC builds a 95% CI for CHF/USD monthly changes:

$$[-0.00152 \pm 1.96 * 0.03184] = [-0.06393; 0.06089].$$

Based on this range for s_t , we derive bounds for the net TE:

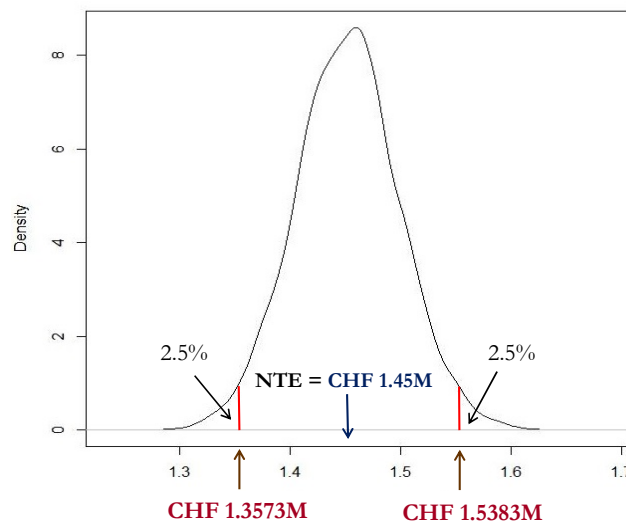
(A) Upper bound

NTE: **USD 1M** * **1.45 CHF/USD** * (1 + 0.06089) = **CHF 1,538,291**.

(B) Lower bound

NTE: **USD 1M** * **1.45 CHF/USD** * (1 + (-0.06393)) = **CHF 1,357,302**.

95% CI range based on a Normal Distribution and VaR(97.5%)



VaR(97.5%): Minimum revenue within a 97.5% C.I.

$$\Rightarrow \text{NTE} \in [\text{CHF } 1.357 \text{ M}; \text{CHF } 1.538 \text{ M}]$$

- The lower bound, for a receivable, represents the worst case scenario within the confidence interval.

There is a *Value-at-Risk* (VaR) interpretation:

VaR: *Maximum expected loss* in a given time interval within a (one-sided) CI.

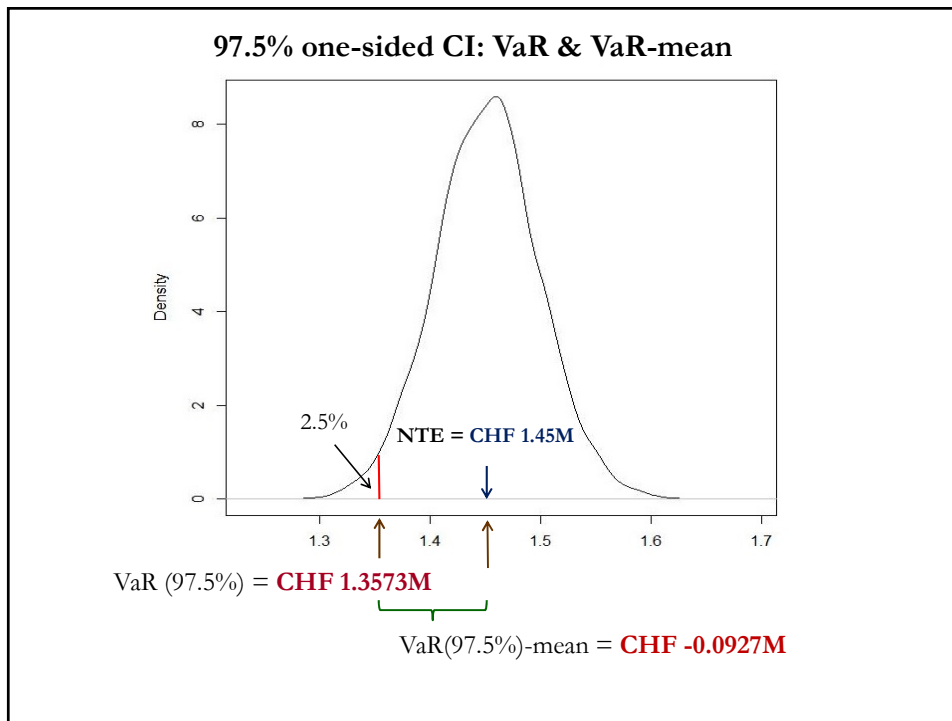
In our case, we can express the “*expected loss*” relative to today’s value:

$$\text{VaR-mean} = \text{VaR} - \text{NTE}$$

Example (continuation): The minimum revenue to be received by SC in the next 30 days, within a 97.5% CI ($\Rightarrow z_{.025} = 1.96$):

$$\begin{aligned} \text{VaR}(97.5\%) &= \text{CHF } 1.45\text{M} [1 + (-0.00152 - 1.96 * 0.03184)] \\ &= \text{CHF } 1,357,302. \end{aligned}$$

$$\Rightarrow \text{VaR-mean} (.975) = \text{CHF } 1.3573\text{M} - \text{CHF } 1.45\text{M} = \text{CHF } -0.0927\text{M}$$



Example (continuation): \Rightarrow NTE \in [CHF 1.357 M; CHF 1.538 M]

VaR(97.5%) = CHF 1,357,302

If SC expects to cover expenses with this USD inflow, the maximum amount in CHF to cover, within a 97.5% CI, should be CHF 1,357,302.

VaR-mean (97.5%) = CHF -0.0927M

Relative to today's valuation (or *expected valuation*, according to RWM), the maximum *expected loss* with a 97.5% "chance" is CHF -0.0927M. ¶

Note: We could have used a different significance level to calculate the VaR, for example 99% ($\Rightarrow z_{.01} = 2.33$). Then,

$$\begin{aligned} \text{VaR}(99\%) &= \text{CHF } 1.45\text{M} [1 + (-0.00152 - 2.33 * 0.03184)] \\ &= \text{CHF } 1.34023. \quad (\text{A more conservative bound.}) \end{aligned}$$

\Rightarrow VaR-mean (.99) = CHF 1.34023M – CHF 1.45M = CHF -0.1098M

• **Summary NTE for Swiss Cruises:**

- NTE = CHF 1.45M

• **NTE Range:**

◇ **Ad-hoc:**

NTE \in [CHF 1.305M; CHF 1.595 M].

◇ **Sensitivity Analysis:**

- Extremes: NTE \in [CHF 1.281 M; CHF 1,6688 M]

- Simulation: NTE \in [CHF 1.3661 M; CHF 1.5443 M]

◇ **Statistical Distribution (normal):**

NTE \in [CHF 1.357 M; CHF 1.538 M]

◆ Approximating Returns

In general, we use *arithmetic returns*: $s_t = S_t/S_{t-1} - 1$. To change the frequency, compounding is needed.

But, if we use *logarithmic returns* –i.e., $s_t = \log(S_t) - \log(S_{t-1})$ –, changing the frequency of mean returns (μ) and return variances (σ^2) is simpler.

Let μ_b & σ_b^2 be measured in a given base frequency, say, b . Then,

$$\begin{aligned}\mu_f &= \mu_b * T, \\ \sigma_f^2 &= \sigma_b^2 * T \quad \Rightarrow \sigma_f = \sigma_b * \text{sqrt}(T)\end{aligned}$$

$T = \#$ periods of base frequency b in new frequency, f .

◆ Approximating Returns – From monthly to daily & annual

Example: Using monthly data, compute daily and annual mean & SD.

From previous Table (base frequency: $b =$ monthly, arithmetic computed):

$$\mu_m = -0.00152$$

$$\sigma_m = 0.03184$$

(1) Daily (i.e., $f = d =$ daily & $T = 1/30$)

$$\mu_d = (-0.00152) * (1/30) = .0000507 \quad (0.006\%)$$

$$\sigma_d = (0.03184) * (1/30)^{1/2} = .00602 \quad (0.60\%)$$

(2) Annual (i.e., $f = a =$ annual & $T = 12$)

$$\mu_a = (-0.00152) * (12) = -0.01824 \quad (-1.82\%)$$

$$\sigma_a = (0.03184) * (12)^{1/2} = 0.110297 \quad (11.03\%)$$

Check: The annual compounded arithmetic return:

$$(1 - 0.00152)^{12} - 1 = -0.01809.$$

When arithmetic returns are low, these approximations work well. ¶

◆ **Approximating Returns – From monthly VaR to annualized VaR**

Example: Using the annualized approximation, we can also approximate an annualized VaR(97.5%) for Swiss Cruises:

$$\begin{aligned} \text{VaR}(97.5\%) &= \text{USD } 1\text{M} * 1.45 \text{ CHF/USD} * [1 + (-.01824 - 1.96 * 0.1103)] \\ &= \text{CHF } 1,101,374. \end{aligned}$$

Note II: Using logarithmic returns rules, we can approximate USD/CHF monthly changes by changing the sign of the CHF/USD, while the variance remains the same.

Then,

- Annualized USD/CHF mean percentage change \approx 1.82%,
- Annualized USD/CHF volatility \approx 11.03%

● **Sensitivity Analysis – Portfolio Approach**

A simulation: Draw different scenarios, pay attention to *correlations!*

Example: IBM has the following CFs in the next 90 days

	Outflows	Inflows	S_t	Net Inflows
GBP	100,000	25,000	1.60 USD/GBP	(75,000)
EUR	80,000	200,000	1.05 USD/EUR	120,000

$$\begin{aligned} \text{NTE}_0 &= \text{EUR } 120\text{K} * 1.05 \text{ USD/EUR} + (\text{GBP } 75\text{K}) * 1.60 \text{ USD/GBP} \\ &= \text{USD } 6,000 \text{ (this is our baseline case)} \end{aligned}$$

Situation 1: Assume $\rho_{\text{GBP, EUR}} = 1$. (EUR and GBP correlation is high.)

Scenario (i): EUR appreciates by 10% against the USD

$$\begin{aligned} \text{Since } \rho_{\text{GBP, EUR}} = 1, \quad S_t &= 1.05 \text{ USD/EUR} * (1 + .10) = 1.155 \text{ USD/EUR} \\ S_t &= 1.60 \text{ USD/GBP} * (1 + .10) = 1.76 \text{ USD/GBP} \end{aligned}$$

$$\begin{aligned} \text{NTE} &= \text{EUR } 120\text{K} * 1.155 \text{ USD/EUR} + (\text{GBP } 75\text{K}) * 1.76 \text{ USD/GBP} \\ &= \text{USD } 6,600. \text{ (+10\% change = USD -600)} \end{aligned}$$

● **Sensitivity Analysis – Portfolio Approach**

Example (continuation): with $\rho_{\text{GBP,EUR}} = 1$.

Scenario (ii): EUR depreciates by 10% against the USD

$$\text{Since } \rho_{\text{GBP,EUR}} = 1, \quad S_t = 1.05 \text{ USD/EUR} * (1 - .10) = 0.945 \text{ USD/EUR}$$

$$S_t = 1.60 \text{ USD/GBP} * (1 - .10) = 1.44 \text{ USD/GBP}$$

$$\text{NTE} = \text{EUR } 120\text{K} * 0.945 \text{ USD/EUR} + (\text{GBP } 75\text{K}) * 1.44 \text{ USD/GBP}$$

$$= \text{USD } 5,400. \quad (-10\% \text{ change} = \text{USD } -600)$$

Now, we can specify a range for NTE

$$\Rightarrow \text{NTE} \in [\text{USD } 5,400; \text{USD } 6,600]$$

Note: The NTE change is exactly the same as the change in S_t . Then,

$$\text{if } \text{NTE}_0 \approx 0 \quad \Rightarrow s_t \text{ has very small effect on NTE.}$$

That is, if a firm has matching inflows and outflows in highly positively correlated currencies, then changes in S_t do not affect NTE. From a risk management perspective, this is very good.

● **Sensitivity Analysis – Portfolio Approach**

Example (continuation):

Situation 2: Suppose the $\rho_{\text{GBP,EUR}} = -1$ (NOT a realistic assumption!)

Scenario (i): EUR appreciates by 10% against the USD

$$\text{Since } \rho_{\text{GBP,EUR}} = -1, \quad S_t = 1.05 \text{ USD/EUR} * (1 + .10) = 1.155 \text{ USD/EUR}$$

$$S_t = 1.60 \text{ USD/GBP} * (1 - .10) = 1.44 \text{ USD/GBP}$$

$$\text{NTE} = \text{EUR } 120\text{K} * 1.155 \text{ USD/EUR} + (\text{GBP } 75\text{K}) * 1.44 \text{ USD/GBP}$$

$$= \text{USD } 30,600. \quad (410\% \text{ change} = \text{USD } 24,600)$$

Scenario (ii): EUR depreciates by 10% against the USD

$$\text{Since } \rho_{\text{GBP,EUR}} = -1, \quad S_t = 1.05 \text{ USD/EUR} * (1 - .10) = 0.945 \text{ USD/EUR}$$

$$S_t = 1.60 \text{ USD/GBP} * (1 + .10) = 1.76 \text{ USD/GBP}$$

$$\text{NTE} = \text{EUR } 120\text{K} * 0.945 \text{ USD/EUR} + (\text{GBP } 75\text{K}) * 1.76 \text{ USD/GBP}$$

$$= (\text{USD } 18,600). \quad (-410\% \text{ change} = \text{USD } -24,600)$$

Now, we can specify a range for NTE

$$\Rightarrow \text{NTE} \in [(\text{USD } 18,600); \text{USD } 30,600]$$

- **Sensitivity Analysis – Portfolio Approach**

Example (continuation):

Note: The NTE has ballooned. A **10% change** in S_t a dramatic increase in the NTE range.

⇒ Having non-matching exposures in different currencies with negative correlation is very dangerous.

Remarks:

- IBM can assume a correlation (estimated from the data). Then, draw many scenarios from a *bivariate normal distribution* to generate a simulated distribution for the NTE.

- Alternatively, IBM can just draw joint pairs from the ED. From this ED, IBM will get a range –and a VaR– for the NTE. ¶

Managing TE

- **A Comparison of External Hedging Tools**

Transaction exposure: Risk from the settlement of transactions in FC.

Example: Imports, exports, acquisition of foreign assets.

- Tools:
 - Futures/forwards (FH)
 - Options (OH)
 - Money market* (MMH)

- Q: Which hedging tool is better?

- New tool: MMH

Money market hedge: Based on a replication of IRPT' arbitrage.

Let's take the case of *receivables* denominated in FC:

- 1) **Borrow FC**
- 2) Convert to DC
- 3) Deposit DC in domestic bank
- 4) **Transfer FC receivable** to cover loan (+ interest) from (1).

Under IRPT, step 4) involves buying FC forward, to repay loan in (1)

⇒ This step is not needed, instead, we just transfer the FC receivable.

Q: Why MMH instead of FH?

- Under perfect market conditions ⇒ MMH = FH
- Under less than perfect conditions ⇒ MMH ≠ FH

- New tool: MMH

Now, let's take the case of *payables* denominated in FC:

- 1) **Borrow DC**
- 2) Convert to FC
- 3) Deposit FC in domestic bank
- 4) **Transfer FC deposit** (+ interest) to cover payable in FC.

Under IRPT, step 4) involves selling FC/buying DC forward, to repay loan in (1)

⇒ This step is not needed, instead, we just transfer the FC deposit.

Q: Why MMH instead of FH?

- Under perfect markets ⇒ MMH = FH
- Under less than perfect markets ⇒ MMH ≠ FH

• **Comparison of Hedging Strategies**

Example: Iris Oil Inc. has a large FC exposure in the form of a CAD cash flow from its Canadian operations. Iris decides to transfer **CAD 300M** to its USD account in 90 days.

FX risk to Iris: CAD may depreciate against the USD.

Data:

$$S_t = 0.8451 \text{ USD/CAD}$$

$$F_{t,90\text{-day}} = 0.8493 \text{ USD/CAD}$$

$$i_{\text{USD}} = 3.92\%$$

$$i_{\text{CAD}} = 2.03\%$$

<u>X</u>	<u>Calls</u>	<u>Puts</u>
.82 USD/CAD	----	0.21
.84 USD/CAD	1.58	0.68
.88 USD/CAD	0.23	----

Example (continuation):

<u>Date</u>	<u>Spot market</u>	<u>Forward market</u>	<u>Money market</u>
t	$S_t = .8451 \text{ USD/CAD}$	$F_{t,90\text{-day}} = .8493 \text{ USD/CAD}$	$i_{\text{USD}} = 3.92\%$ $i_{\text{CAD}} = 2.03\%$

$t + 90$ Receive **CAD 300M** and transfer into USD.

$$\text{NTE} = \text{CAD } 300\text{M} * .8451 \text{ USD/CAD} = \text{USD } 253.53\text{M}$$

• **Hedging Strategies:**

1. Do Nothing

Do not hedge and exchange the **CAD 300M** at S_{t+90} .

2. Forward Market

At t , sell the **CAD 300M** forward and at time $t + 90$ guarantee:

$$\text{CAD } 300\text{M} * .8493 \text{ USD/CAD} = \text{USD } 254,790,000$$

Example (continuation):**3. Money Market**

At t , Iris Oil takes the following three steps, simultaneously:

- 1) Borrow from Canadian bank at **2.03%** for 90 days :

$$\text{CAD } 300\text{M} / [1 + .0203 * (90/360)] = \text{CAD } 298,485,188.$$

- 2) Convert to USD at S_t :

$$\text{CAD } 298,485,188 * 0.8451 \text{ USD/CAD} = \text{USD } 252,249,832$$

- 3) Deposit in US bank at **3.92%** for 90 days to guarantee at time $t+90$:

$$\text{USD } 252,249,832 * [1 + .0392 * (90/360)] = \text{USD } 254,721,880.$$

Note: Both the FH and the MMH guarantee certainty at time $t+90$

FH delivers to Iris Oil: **USD 254,790,000**

MMH delivers to Iris Oil: **USD 254,721,880**

\Rightarrow Iris Oil selects the FH. (MMH is a *dominated* strategy.)

Example (continuation):**4. Option Market**

At t , buy a **put**. Available 90-day options:

X	Calls	Puts
.82 USD/CAD	----	0.21
.84 USD/CAD	1.58	0.68
.88 USD/CAD	0.23	----

Buy the **.84 USD/CAD put** \Rightarrow Total premium cost of **USD 2.04M**.

Position	Initial CF	Cash flows at $t+90$	
		$S_{t+90} < .84 \text{ USD/CAD}$	$S_{t+90} > .84 \text{ USD/CAD}$
Option (HP)	USD 2.04M	$(.84 - S_{t+90}) * \text{CAD } 300\text{M}$	0
Underlying (UP)	0	$S_{t+90} * \text{CAD } 300\text{M}$	$S_{t+90} * \text{CAD } 300\text{M}$
Total CF	USD 2.04M	USD 252M	$S_{t+90} \text{ CAD } 300\text{M}$

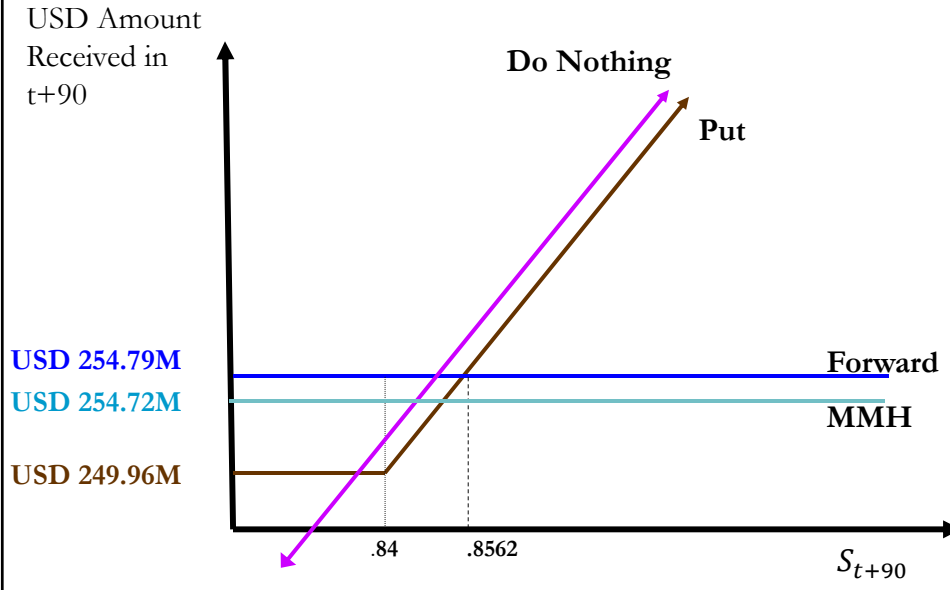
Net CF at $t + 90$:

$$\text{USD } 249,960,000 \quad \text{for } S_{t+90} < .84 \text{ USD/CAD}$$

$$\text{or } S_{t+90} * \text{CAD } 300\text{M} - \text{USD } 2.04\text{M} \quad \text{for } S_{t+90} > .84 \text{ USD/CAD}$$

Example (continuation):

- Let's plot all strategies:



Example (continuation): Companies do not like paying premiums.

5. Collar

At time t , *buy* a **put** and *sell* a **call**.

Buy **.84** put at **USD 0.0068**

Sell **.88** call at **USD 0.0023**. \Rightarrow Initial cost = **USD 0.0045** per collar

\Rightarrow Total cost: **USD 1.35M**

Position	Initial CF	Cash flows at t+90		
		$S_{t+90} < .84$	$.84 < S_{t+90} < .88$	$S_{t+90} > .88$
Put	USD 2.04M	$(.84 - S_{t+90}) * \text{CAD } 300\text{M}$	0	0
Call	-USD 0.69M	0	0	$(.88 - S_{t+90}) * \text{CAD } 300\text{M}$
UP	0	$S_{t+90} * \text{CAD } 300\text{M}$	$S_{t+90} * \text{CAD } 300\text{M}$	$S_{t+90} * \text{CAD } 300\text{M}$
Total CF	USD 1.35M	USD 252M	$S_{t+90} \text{ CAD } 300\text{M}$	USD 264M

Net CF at $t + 90$:

$\text{USD } 250.65\text{M}$ for $S_{t+90} < .84 \text{ USD/CAD}$
 or $S_{t+90} \text{ CAD } 300\text{M} - \text{USD } 1.35\text{M}$ for $.84 \text{ USD/CAD} < S_{t+90} < .88 \text{ USD/CAD}$
 or $\text{USD } 262.65\text{M}$ for $S_{t+90} > .88 \text{ USD/CAD}$

Note: This collar reduces the upside: establishes a floor and a cap.

Example (continuation):

6. Alternative: Zero cost insurance:

At time t , *buy* puts and *sell* calls with overall (or \approx) matching premium.

Buy **.84 put**

Sell 3 **.88 calls**. \Rightarrow Initial cost ≈ 0 (actually, a small profit. We'll ignore it).

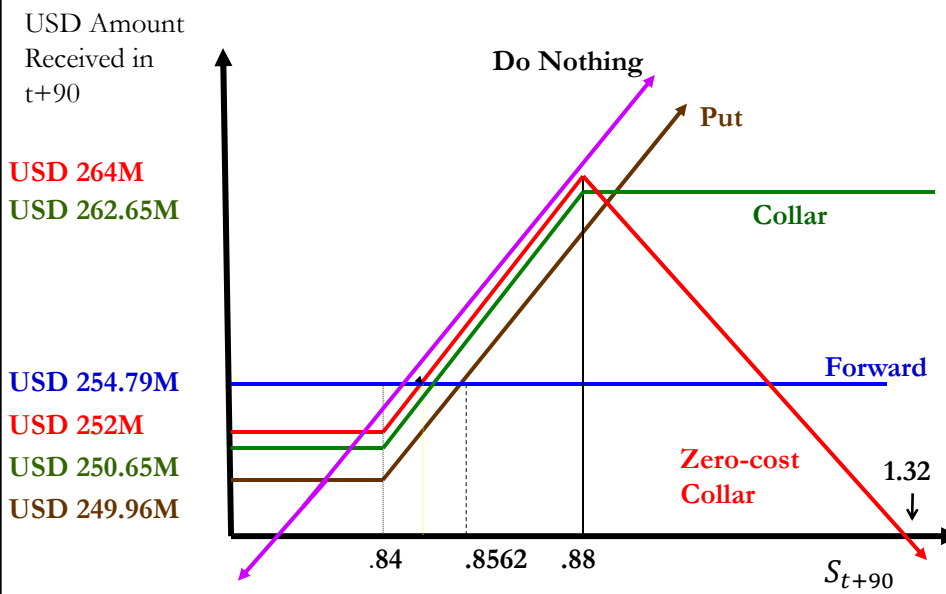
Position	Cash flows at $t+90$		
	$S_{t+90} < .84$	$.84 < S_{t+90} < .88$	$S_{t+90} > .88$
Put	$(.84 - S_{t+90}) * \text{CAD } 300\text{M}$	0	0
3 Calls	0	0	$3 * (.88 - S_{t+90}) * \text{CAD } 300\text{M}$
UP	$S_{t+90} * \text{CAD } 300\text{M}$	$S_{t+90} * \text{CAD } 300\text{M}$	$S_{t+90} * \text{CAD } 300\text{M}$
Total CF	USD 252M	$S_{t+90} \text{ CAD } 300\text{M}$	USD 792M - $2 * S_{t+90} \text{ CAD } 300\text{M}$

Net CF at $t + 90$:

USD 252M for all $S_{t+90} < .84 \text{ USD/CAD}$
 or $S_{t+90} \text{ CAD } 300\text{M}$ for $.84 \text{ USD/CAD} < S_{t+90} < .88 \text{ USD/CAD}$
 or USD 792 M - $2 S_{t+90} \text{ CAD } 300\text{M}$ for all $S_{t+90} > .88 \text{ USD/CAD}$

Example (continuation):

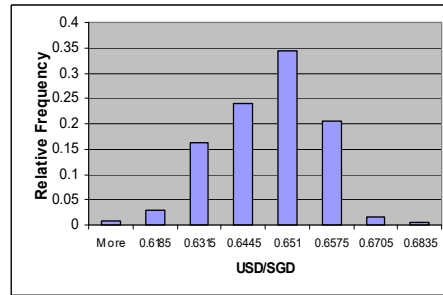
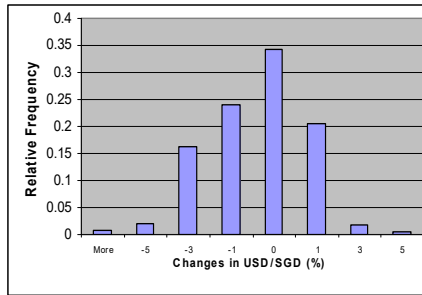
Let's plot all strategies:



• **Optimal Hedging Strategies?**

Q: Which strategy is better? We need to say something about S_{t+90} . For example, we can assume a distribution (normal) or use the ED to say something about future changes in S_t .

Example: Suppose we have a **receivable in SGD** in 30 days. We can use the **distribution** for monthly USD/SGD changes from the past 30 years. Then, we get the distribution for S_{t+30} (USD/SGD).



Example (continuation): Distribution of monthly USD/SGD changes from past 30 years. Raw data & relative frequency for S_{t+30} (USD/SGD).

s_t (SGD/USD)	Frequency	Rel frequency	$S_t = 1/.65*(1+s_t)$	
-0.0494 or less	2	0.0058	1.462	0.6838
-0.0431	2	0.0058	1.472	0.6793
-0.0369	1	0.0029	1.482	0.6749
-0.0306	3	0.0087	1.491	0.6705
-0.0243	6	0.0174	1.501	0.6662
-0.0181	20	0.0580	1.511	0.6620
-0.0118	36	0.1043	1.520	0.6578
-0.0056	49	0.1420	1.530	0.6536
0.0007	86	0.2493	1.540	0.6495
0.0070	52	0.1507	1.549	0.6455
0.0132	41	0.1188	1.559	0.6415
0.0195	29	0.0841	1.568	0.6376
0.0258	5	0.0145	1.578	0.6337
0.0320	7	0.0203	1.588	0.6298
0.0383	5	0.0145	1.597	0.6260
0.0446	0	0.0000	1.607	0.6223
0.0508 or +	3	0.0058	1.617	0.6186

• **Examples assuming an explicit distribution for S_{t+T}**

Example – Receivables: Evaluate (1) FH, (2) MMH, (3) OH & (4) NH.

Cud Corp will receive **SGD 500,000** in 30 days. (SGD Receivable.)

Data:

- $S_t = .6500 - .6507$ USD/SGD.
- $F_{t,30} = .6510 - .6519$ USD/SGD.
- 30-day interest rates: $i_{\text{SGD}}: 2.65\% - 2.75\%$ & $i_{\text{USD}}: 3.20\% - 3.25\%$
- A 30-day put option on SGD: $X = .65$ USD/SGD and $P_t = \text{USD}.01$.
- Forecasted S_{t+30} :

Possible Outcomes	Probability
USD .63	18%
USD .64	24%
USD .65	34%
USD .66	21%
USD .68	3%

(1) FH: Sell SGD 30 days forward

$$\begin{aligned} \text{USD received in 30 days} &= \text{Receivables in SGD} * F_{t,30} \\ &= \text{SGD } 500,000 * .651 \text{ USD/SGD} = \text{USD } 325,500. \end{aligned}$$

(2) MMH:

- Borrow SGD at **2.75%** for 30 days,
- Convert to USD at **.65 USD/SGD**,
- Deposit USD at **3.2%** for 30 days,
- Repay SGD loan in 30 days with SGD 500,000 receivable

$$\begin{aligned} \text{Amount to borrow} &= \text{SGD } 500,000 / (1 + .0275 * 30/360) = \\ &= \text{SGD } 498,856.79 \end{aligned}$$

$$\begin{aligned} \text{Convert to USD (Amount to deposit in U.S. bank)} &= \\ &= \text{SGD } 498,856.79 * .65 \text{ USD/SGD} = \text{USD } 324,256.91 \end{aligned}$$

$$\begin{aligned} \text{Amount received in 30 days from U.S. bank deposit} &= \\ &= \text{USD } 324,256.91 * (1 + .032 * 30/360) = \text{USD } 325,121.60 \end{aligned}$$

(3) OH: Purchase put option.

$$X = .65 \text{ USD/CHF}$$

$$P_t = \text{premium} = \text{USD } .01$$

Possible S_{t+30}	Premium per SGD + Op Cost	Exercise?	Net USD Received for SGD 0.5M	Prob
.63 USD/SGD	USD .010027	Yes	USD 319,986.5	18%
.64 USD/SGD	USD .010027	Yes	USD 319,986.5	24%
.65 USD/SGD	USD .010027	No	USD 319,986.5	34%
.66 USD/SGD	USD .010027	No	USD 324,986.5	21%
.68 USD/SGD	USD .010027	No	USD 334,986.5	3%

Note: In the Total Amount Received (in USD) we have subtracted the *opportunity cost* involved in the upfront payment of a premium:

$$\text{USD } .01 * .032 * 30/360 = \text{USD } .000027 \quad (\text{Total} = \text{USD } 13.50)$$

$$\Rightarrow \text{Total Premium Cost: USD } 5,013.50$$

$$E[\text{Amount Received in USD}] = 319,986.5 * .76 + 324,986.50 * .21 + 334,986.50 * .03 = \text{USD } 321,486.5$$

(4) No Hedge (NH): Sell **SGD 500,000** in the spot market in 30 days.

Possible S_{t+30}	USD Received for SGD 0.5M	Probability
.63 USD/SGD	USD 0.315M	18%
.64 USD/SGD	USD 0.320M	24%
.65 USD/SGD	USD 0.325M	34%
.66 USD/SGD	USD 0.330M	21%
.68 USD/SGD	USD 0.340M	3%

Note: When we compare (1) to (4), it's not clear which one is better. Preferences will matter. We can calculate an expected value:

$$E[\text{Amount Received in USD}] = 315K * .18 + 320K * .24 + 325K * .34 + 330K * .21 + 335K * .03 = \text{USD } 323,500$$

Conclusion: Cud Corporation is likely to choose the FH. But, risk preferences matter. ¶

Example – Payables: Evaluate (1) FH, (2) MMH, (3) OH, (4) No Hedge
Situation: Cud Corp needs **CHF 100,000** in 180 days. (CHF Payable.)

Data:

- $S_t = .675 - .680$ USD/CHF.
- $F_{t,180} = .695 - .700$ USD/CHF.
- 180-day interest rates are as follows:
 - i_{CHF} : 9% - 10%;
 - i_{USD} : 13% - 14.0%
- A 180-day call option on CHF: $X = .70$ USD/CHF and $P_t = \text{USD}.02$.
- Cud forecasted S_{t+180} :

Possible Outcomes	Probability
USD .67	30%
USD .70	50%
USD .75	20%

(1) FH: Purchase CHF 180 days forward

$$\text{USD needed in 180 days} = \text{Payables in CHF} \times F_{t,180} \\ = \text{CHF } 100,000 * .70 \text{ USD/CHF} = \text{USD } 70,000.$$

(2) MMH:

- Borrow USD at 14% for 180 days,
- Convert to CHF at .680 USD/CHF ,
- Invest CHF at 9% for 180 days,
- Repay USD loan in 180 days & transfer CHF deposit to cover payable

$$\text{Amount in CHF to be invested} = \text{CHF } 100,000 / (1 + .09 * 180/360) \\ = \text{CHF } 95,693.78$$

$$\text{Amount in USD needed to convert into CHF for deposit} = \\ = \text{CHF } 95,693.78 * .680 \text{ USD/CHF} = \text{USD } 65,071.77$$

$$\text{Interest and principal owed on USD loan after 180 days} = \\ = \text{USD } 65,071.77 * (1 + .14 * 180/360) = \text{USD } 69,626.79$$

(3) OH: Purchase call option. $X = .70 \text{ USD/CHF}$
 $C_t = \text{premium} = \text{USD } .02.$

Possible S_{t+180}	Premium per CHF + Op Cost	Exercise?	Net Paid for CHF 0.1M	Prob
.67 USD/SGD	USD .0213	No	USD 69,130	30%
.70 USD/SGD	USD .0213	No	USD 72,130	50%
.75 USD/SGD	USD .0213	Yes	USD 72,130	20%

Note: In the Total USD Cost we have included the opportunity cost involved in the upfront payment of a premium = **USD 130.**

$E[\text{Amount to Pay in USD}] = \text{USD } 71,230$

• *Preferences matter:* A risk taker may like the 30% chance of doing better with the OH than with the MMH.

(4) Remain Unhedged: Purchase **CHF 100,000** in 180 days.

Possible S_{t+180}	Net Paid for CHF 0.1M	Probability
.67 USD/SGD	USD 67,000	30%
.70 USD/SGD	USD 70,000	50%
.75 USD/SGD	USD 75,000	20%

Preferences matter: Again, a risk taker may like the **30% chance** of doing better with the NH than with the MMH. (Actually, there is also an additional 50% chance of being very close to the MMH.)

$E[\text{Amount to Pay in USD}] = \text{USD } 70,100$

Conclusion: Cud Corporation is likely to choose the MMH. ¶

Internal Methods

- These are hedging methods that do not involve financial instruments.

- **Risk Shifting**

Q: Can firms completely avoid FX exposure?

A: Yes! By **pricing** all foreign transactions in **domestic currency**.

Example: Bossio Co., a U.S. firm, sells naturally colored cotton. Asuni, a Japanese company, buys Bossio's cotton. Bossio Co. prices all exports in USD. ¶

⇒ Currency risk is not eliminated. The foreign company bears it.

- Problem with risk-shifting: Reduces firm flexibility.

- **Currency Risk Sharing**

Two parties agree -with a customized hedge contract- to **share** the **FX risk** in a transaction.

Example: Asuni buys cotton for **USD 1 million** from Bossio Co.

Risk Sharing agreement:

- If $S_t \in [100 \text{ JPY/USD}; 140 \text{ JPY/USD}] \Rightarrow$ Transaction unchanged. (Asuni pays **USD 1 M** to Bossio Co.)

- If $S_t < 100 \text{ JPY/USD}$ or $S_t > 140 \text{ JPY/USD} \Rightarrow$ parties share risk equally

Suppose that when Asuni has to pay Bossio Co., $S_t = 180 \text{ JPY/USD}$.

Then, settlement $S_t = 160 \text{ JPY/USD} (= 180 - 40/2)$.

Asuni's final cost = JPY 160 million = USD 888,889 < **USD 1M**.

Note: Range where the transaction is unchanged is called *neutral zone*. ¶

- **Leading and Lagging (L&L)**

Firms can reduce FX exposure by **accelerating** or **decelerating the timing** of payments that must be made in different currencies:

⇒ **Leading** or **Lagging** the movement of funds.

L&L is done between the parent company and its subsidiaries or between two subsidiaries.

Example: Parent company: HAL (U.S. company).

Subsidiaries: Mexico, Brazil, and Hong Kong.

HAL Hong Kong's exposure is too large.

HAL orders HAL Mexico and HAL Brazil to accelerate (*lead*) payments to HAL Hong Kong. ¶

- L&L changes assets/liabilities in one firm, with reverse effect on the other firm.

⇒ L&L changes balance sheet positions.

Might be a good tool for achieving a hedged balance sheet position.

- **Funds Adjustments**

Key to hedging:

Match inflows & outflows denominated in the FC.

Chinese subsidiary in U.S.
with **CF > 0** in USD

Increase USD purchases

Decrease CNY purchases

Decrease USD sales

Increase CNY sales

Increase USD borrowing

Reduce CNY borrowing

Italian subsidiary in U.S.
with **CF < 0** in USD

Decrease USD purchases

Increase EUR purchases

Increase USD sales

Decrease EUR sales

Reduce USD borrowing

Increase EUR borrowing

Example: Japanese and German carmakers have built plants in the U.S.

Economic Exposure

Economic exposure (EE): Risk associated with a change in the NPV of a firm's expected cash flows, due to an *unexpected* change in S_t .

Note: S_t is very difficult to forecast. Actual change in S_t can be considered “unexpected.”

- General definition: It can be applied to any firm (domestic, MNC, exporting, importing, purely domestic, etc.).
- The degree of EE depends on:
 - Type & structure of the firm
 - Industry structure in which the firm operates.

- In general:
 - **Importing & exporting** firms face **higher** EE than purely domestic firms
 - **Monopolistic** firms face **lower** EE than firms that operate in competitive markets.

Example: A U.S. firm face almost no competition in domestic market. Then, it can transfer to prices almost any increase of its costs due to changes in S_t . Thus, this firm faces no/low EE. ¶

- The degree of EE for a firm is an empirical question.
- Economic exposure is difficult to measure.
- We can use *accounting data* (EAT changes) or *financial/economic data* (returns) to measure EE. Economists like economic-based measures.

Measuring Economic Exposure

A Measure Based on Accounting Data

We use cash flows to estimate FX exposure. For example, we simulate a firm's **CFs** (EBT, Operating Income, etc.) **under several FX scenarios**.

Example: IBM HK provides the following info:

Sales and cost of goods are dependent on S_t :

$$S_t = 7 \text{ HKD/USD} \quad S_t = 7.70 \text{ HKD/USD}$$

Sales (in HKD)	300M	400M
Cost of goods (in HKD)	<u>150M</u>	<u>200M</u>
Gross profits (in HKD)	150M	200M
Interest expense (in HKD)	<u>20M</u>	<u>20M</u>
EBT (in HKD)	130M	180M

Example (continuation):

A **10% depreciation** of the HKD **increases** HKD CFs from **HKD 130M** (=USD 18.57M) to **HKD 180M** (=USD 23.38M): A **25.92%** change in CFs measured in USD.

Q: Is EE **significant**?

A: We can calculate the elasticity of CF to changes in S_t :

$$\text{CF elasticity} = \frac{\% \text{ change in EBT}}{\% \text{ change in } S_t} = \frac{.2592}{.10} = 2.59$$

Interpretation: We say, a 1% depreciation of the HKD produces a change of **2.59%** in EBT. Quite significant. But the change in exposure is **USD 4.81M**. This amount may not be significant for IBM (*Judgment call* needed.)

IBM HK behaves like a net exporter: Weaker DC, Higher CFs. ¶

Note: Firms will simulate many scenarios & produce an expected value.

We can use historical accounting cash flows to calculate economic exposure.

Example: Kellogg's cash flow elasticity in 2020-2019.

From 2019 to 2020 (end-of-year to end-of-year), K's operating income increased **2.6%**. The USD depreciated against basket of major currencies by **3.58%**. Then,

$$\text{CF elasticity} = \frac{.026}{.0358} = 0.73$$

Interpretation: We say, a 1% depreciation of the USD produces a positive change of **0.73%** in operating income. K's behaves like a **net exporter**. ¶

A Regression based Measure and a Test

CF elasticity gives us a measure, but it is not a test of EE. A judgment call is needed.

It is easy to **test** regression coefficients (t-tests or F-tests).

• Simple steps:

(1) Get data: CF_t & S_t (available from the firm's past)

(2) Estimate regression:

$$\Delta CF_t = \alpha + \beta \Delta S_t + \varepsilon_t,$$

⇒ β : Sensitivity of ΔCF_t to ΔS_t .

⇒ The higher β , the greater the impact of ΔS_t on CF_t .

(3) Test for EE ⇒ H_0 (no EE): $\beta = 0$

H_1 (EE): $\beta \neq 0$

(4) Evaluation of this regression: t-statistic of β and R^2 .

Rule: $|t_\beta = \beta / \text{SE}(\beta)| > 1.96$ ⇒ β is significant at the 5% level.

A Regression based Measure and a Test

In general, regression is done in terms of % changes:

$$cf_t = \alpha + \beta s_t + \xi_t$$

cf_t : % change in CF from t-1 to t.

Interpretation of β : A 1% change in S_t changes the CF_t by $\beta\%$.

• Expected Signs

We estimate the regression from a Domestic (say, U.S.) firm's point of view: CF measured in DC (say, USD & S_t is USD/FC). Then, from the regression, we can derive the Expected sign (β):

Type of company	Expected sign for β
U.S. Importer	Negative
U.S. Exporter	Positive
Purely Domestic	Depends on industry

• Other variables also affect CFs: Investments, acquisitions, growth of the economy, etc.

We “control” for the other variables that affect CFs with a multivariate regression, say with k other variables:

$$cf_t = \alpha + \beta s_t + \delta_1 X_{1,t} + \delta_2 X_{2,t} + \dots + \delta_k X_{k,t} + \varepsilon_t$$

where $X_{k,t}$ represent one of the k^{th} other variables that affects CFs.

Note: Sometimes the impact of ΔS_t is not felt immediately.

⇒ contracts and short-run costs matter.

Example: For an exporting U.S. company a sudden appreciation of the USD increases CF in the short term. Solution: use a modified regression:

$$cf_t = \alpha + \beta_0 s_t + \beta_1 s_{t-1} + \beta_2 s_{t-2} + \dots + \beta_q s_{t-q} + \delta_1 X_{1,t} + \dots + \varepsilon_t$$

Sum of β 's: Total sensitivity of cf_t to s_t ($= \beta_0 + \beta_1 + \beta_2 + \beta_3 + \dots$)

A Measure Based on Financial Data

Accounting data can be manipulated. Moreover, international comparisons are difficult. Instead, use financial data: Stock prices!

We can easily measure how returns and ΔS_t move together: *correlation*.

Example: Kellogg's and IBM's EE.

Using monthly stock returns for Kellogg's ($r_{K,t}$) and monthly changes in S_t (USD/EUR) from **33 years (1988:Jan – 2022:Jan)**, we estimate $\rho_{K,s}$ (correlation between $r_{K,t}$ & s_t) = **0.150**. It looks small.

We do the same exercise for IBM, measuring the correlation between $r_{IBM,t}$ & s_t , obtaining $\rho_{IBM,s}$ = **0.089**, small and, likely, close to zero.

But, if we use USD/TWC, based on the major currencies, things change a bit: $\rho_{K,s}$ = **0.1263** (similar to USD/EUR) & $\rho_{IBM,s}$ = **0.1795** (different). ¶

An Easy Measure of EE Based on Financial Data

- Better measure: A regression-based measure that can be used as a test.

Steps:

- 1) Regress, r_t , returns against (unexpected) ΔS_t .

$$r_t = \alpha + \beta s_t + \varepsilon_t$$

- 2) Check statistical significance of regression coefficient for s_t :

$$H_0 \text{ (No EE): } \beta = 0.$$

$$H_1 \text{ (EE): } \beta \neq 0.$$

⇒ A simple t-test can be used to test H_0 .

Interpretation: A 1% change in S_t changes the Value of the firm by $\beta\%$.

Example: Kellogg's EE.

Using **1988-2022** data (see previous example), we run the regression:

$$r_{K,t} = \alpha + \beta s_t (\text{USD/TWC}) + \varepsilon_t$$

$R^2 = 0.01596$

Standard Error = 5.56447

Observations = 409

	<i>Coefficients</i>	<i>Standard Error</i>	<i>t-stat</i>	<i>P-value</i>
Intercept (α)	0.38592	0.27515	1.4026	0.1615
s_t (β)	0.43775	0.17041	2.5688	0.0106

Analysis: Reject H_0 , $|t_\beta = 2.57| > 1.96$ (significantly $\neq 0$) \Rightarrow EE!

$\beta > 0$, K behaves like an exporter.

Interpretation of β : A 1% increase in exchange rates, increases K's returns by **0.44%**.

Note: R^2 is very low! ¶

Example: IBM's EE.

Now, using the IBM data (**1988-2022**), we run the regression:

$$r_{IBM,t} = \alpha + \beta s_t (\text{USD/TWC}) + \varepsilon_t$$

$R^2 = 0.03221$

Standard Error = 7.4465

Observations = 409

	<i>Coefficients</i>	<i>Standard Error</i>	<i>t-stat</i>	<i>P-value</i>
Intercept (α)	0.38896	0.36821	1.0563	0.2914
s_t (β)	0.83941	0.22805	3.6809	0.0003

Analysis: Reject H_0 , $|t_\beta = 3.68| > 1.96$ (significantly $\neq 0$) \Rightarrow EE!

$\beta > 0$, DIS behaves like an exporter.

Interpretation of β : A 1% increase in exchange rates, increases DIS's returns by **0.84%**.

Again, the R^2 is low! ¶

• Returns are not only influenced s_t . In investments, it is common to use the 3 factors from the **Fama-French models** to model stocks returns:

- **Market** ($[r_M - r_f]$)
- **SMB** (size)
- **HML** (value).

In Kellogg's case:

$$r_{K,t} = \alpha + \gamma_1 (r_M - r_f)_t + \gamma_2 \text{SMB}_t + \gamma_3 \text{HML}_t + \varepsilon_t$$

A momentum can be added to accommodate Carhart's (1997) model.

Note: In general, we find γ_1 & γ_3 significant. R^2 is not very high.

• Now, we test if Kellogg's faces EE, *conditioning* on the other drivers of K's returns. That is, we do a t-test on β on the following regression:

$$r_{K,t} = \alpha + \gamma_1 (r_{\text{Mar}} - r_{f,t}) + \gamma_2 \text{SMB}_t + \gamma_3 \text{HML}_t + \beta s_t + \varepsilon_t$$

Example (continuation): Kellogg's EE (with 3 FF factors):

	Coefficients	Std Error	t-stat
Intercept	0.0798	0.2691	0.2967
Market ($R_m - R_f$)	0.3893	0.0647	6.0204
Size (SMB)	-0.1144	0.0898	-1.2738
B-M (HML)	0.1546	0.0851	1.8157
s_t (β)	0.2601	0.1664	1.5633

$R^2 = 0.0995$ (a higher value driven mainly by the market factor).

Now, t-stat = **1.56** (*p-value* = .119). We say:

"After controlling for other factors that affect Kellogg's excess returns, we do not find evidence of EE at the 5% significance level."

⇒ Usual interpretation: No EE for K.

We also see a lower sensitivity, β : **0.2601**. ¶

Example (continuation): IBM's EE (with 3 FF factors):

	Coefficients	Std Error	t-stat
Intercept	-0.2894	0.3180	-0.9102
S_t (β)	0.3963	0.1966	2.0157
Market ($R_m - R_f$)	0.9506	0.0764	12.4363
Size (SMB)	-0.2557	0.1062	-2.4085
B-M (HML)	-0.1154	0.1006	-1.1471

$R^2 = 0.3092$.

The t-stat = **2.01** (p -value = .045).

⇒ Usual interpretation: IBM faces EE.

Again, we see a big reduction in lower sensitivity, β : **0.3963**. ¶

EE: Evidence

The above regression (for K) has been done for firms around the world.

Results from work by Ivanova (2014):

- Mean $\beta = 0.57$ (a 1% USD depreciation increases returns by 0.57%).
- But, only **40%** of the EE are *statistically significant* at the 5% level.
- For large firms (MNCs), EE is small –average $\beta = 0.063$ – & **not significant** at the 5% level.
- **52%** of the EEs come from U.S. firms that have no international transactions (a higher S_t “protects” these domestic firms).

Summary:

- On average, large companies (MNCs, Fortune 500) face no EE.
- EE is a problem of small and medium, undiversified firms.

EE: Evidence

- Check Ivanova's results for big firms, using the **S&P 100**.

We regress SP100 returns from past **38 years (1984:Apr – 2022:Jan)** against s_t (USD/TWC) & the 3 FF factors:

$R^2 = 0.9664$

Standard Error = 0.8136

Observations = 454

	Coefficients	Std Error	t-stat	P-value
Intercept	-0.0247	0.0389	-0.6357	0.5253
s_t	-0.0225	0.0231	-0.9756	0.3298
Market - r_f	0.9988	0.0090	110.5233	>.00001
SMB	-0.2459	0.0133	-18.4659	>.00001
HML	0.0068	0.0126	0.5381	0.5907

Since $|t_{\beta} = -0.98| < 1.96 \Rightarrow$ No evidence of EE for big U.S. firms.

CASE 2 – Hedging TE (Payable)

- Two parts
 - **Group assignment** (DW's hedging problem)
 - **Class assignment**

- **Group assignment**

DW ordered Japanese parts valued at **JPY 200M**.

Payment: Delivery usually takes two months. Payment is due within **30 days** of delivery (*tentative* delivery payment date **April 17**).

PART I

Today: **December 6**, DW evaluates risk & hedging strategies.

- Risk evaluation: Construct Ranges, VaR
- Hedging strategies: Options, & Forwards.

- **Group assignment (continuation)**

PART II

Today: **May 6**. Parts arrived on April 11. Payment is due in five days (**May 11**). Evaluate cost of different hedging strategies.

- **Class assignment**

Get JPY/USD FX rate data from my homepage ([database2.xlsx](#)).

- ◊ Evaluate Risk, with **10 years of data** (adjust monthly frequency to **5-mo**):
 - Construct a VaR (97.5%) assuming a Normal distribution
 - Worst/Best Case Scenarios
 - Construct a VaR (97.5%) using a simulation
- ◊ On **December 6, 2012**, you do a 6-mo futures hedge. DW buys the JPY Dec futures contract. Value this contract on **May 6, 2013**.
- ◊ On **December 6, 2012**, you do a 6-mo MM hedge. Calculate the cost on **May 6, 2013**. (Need to discount CFs back to May 6, 2013.)