

**Homework 2** (Due September 28)

Instructions: Send your solved homework, along with the code, to my TA, Yousaf, Hammad. His email address is: hyousaf@CougarNet.UH.EDU.

**1.1 (Tests of Hypothesis).** Download the Shiller dataset (Shiller\_data.csv) from my homepage. Or just cut-and-paste the following line:

```
Sh_da <- read.csv("http://www.bauer.uh.edu/rsusmel/4397/Shiller_data.csv", head=TRUE, sep=",")
```

You have stock prices (P), dividends (D), earning (E), consumer prices (CPI) and long interest rates (Long\_i). Regress log stock returns,  $r_i$ , against log earning changes,  $earn_i$ , inflation rate (in log changes),  $Inf_i$ , and interest rates,  $int_i$  (need to subtract one observation):

$$r_i = \beta_0 + \beta_1 earn_i + \beta_2 Inf_i + \beta_3 int_i + \varepsilon_i$$

- Report the regression
- Interpret the  $R^2$ .
- Interpret the estimated coefficient  $\beta_1$ .
- Test with a goodness of fit test  $H_0: \beta_1 = \beta_2 = \beta_3 = 0$ .
- Test with an F-test  $H_0: \beta_1 = \beta_3 = 0$ .
- Test with a Wald test  $H_0: \beta_2 = 0.5$  and  $\beta_3 = -0.1$
- Check if the model shows structural change at  $T_{SB} = \text{October 1973}$ . Perform a Chow test.

**1.2 (Bootstrapping).** Bootstrap the t-statistics in the above regression, with  $B = 1,000$ .

- Report the mean and the bias in your estimation for each parameter.
- Build a 95% C.I. for  $\beta_2$ .

**1.3 (Non-nested Tests)** Download the Stocks\_FX\_1973 dataset (Stocks\_FX\_1973.csv).

- Estimate two Fama-French 3-factor model for GE returns: One with Mkt\_RF, SMB and HML (Model 1) and the other with Mkt\_RF, CMA and RMW.
- Use a J-test to select a model.
- Perform an encompassing test to select or favor a model.

**1.4 (Structural Change)**

- Explain the term ‘parameter structural stability’?
- A financial econometrician thinks that the stock market crash of October 1987 fundamentally changed the risk–return relationship given by the CAPM equation. He decides to test this hypothesis using a Chow test. The model is estimated using monthly data from January 1981–December 1995, and then two separate regressions are run for the sub-periods corresponding to data before and after the crash. The model is

$$r_t = \alpha + \beta r_{mt} + \varepsilon_t$$

so that the excess return on a security at time  $t$  is regressed upon the excess return on a proxy for the market portfolio at time  $t$ . The results for the three models estimated for a given stock are as follows:

1981M1–1995M12

$$r_t = 0.0215 + 1.491 r_{mt} \quad RSS = 0.189 \quad T = 180$$

1981M1–1987M10

$$r_t = 0.0163 + 1.308 r_{mt} \quad RSS = 0.079 \quad T = 82$$

1987M11–1995M12

$$r_t = 0.0360 + 1.613 r_{mt} \quad RSS = 0.082 \quad T = 98$$

- c. What are the null and alternative hypotheses that are being tested here, in terms of  $\alpha$  and  $\beta$ ?
- d. Perform the test. What is your conclusion?

### 1.5 (Theory Review)

- a. What does it mean that an estimator is unbiased? Consistent? Would you ever consider an inconsistent estimator?
- b. Suppose you suspect the unobservable error terms ( $\varepsilon$ ) in a regression does not follow a Normal distribution. Describe how would you test that  $\varepsilon$  is not normally distributed (state the Null Hypothesis and the test used).
- c. Under what circumstances you would use a bootstrap to compute SE for a regression?
- d. What are the consequences for the CLM that the errors are not normally distributed?
- e. What does it mean that a regression suffer from multicollinearity? What is the possible effect of multicollinearity on a regression? Can you fix it?
- f. Describe the omitted variables and irrelevant variables problem. What are the properties of OLS under both scenarios?