

# Chapter 18

## SWAPS

### A - Types and Valuation

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#### • Last Class

##### International Bond Markets

- ◊ Eurobond + Foreign Bond Market = International Bond Market (30%)
- ◊ Eurobond: Same structure as a domestic bond, but *bearer* securities are OK and *mainly unregulated*
- ◊ Many Instruments in Eurobond Markets (most popular one: fixed bond)
- ◊ Pricing of a new bond –i.e., setting YTM. Key is finding the right benchmark.
- ◊ Different cases:
  - Established company with borrowing history:
 
$$YTM_{\text{new debt}} = YTM_{\text{outstanding}}$$
  - Established company with no borrowing history:
 
$$YTM_{\text{new debt}} = YTM_{\text{benchmark similar companies}}$$
  - New company in new industry:
 
$$YTM_{\text{new debt}} = YTM_{\text{book building/general benchmark}}$$

- **This Class**

- Swaps

- ◊ Definition
- ◊ Different Types: Interest Rate, Currency, Equity, Commodity & CDS.
- ◊ Market Organization and Swap Dealers
- ◊ Uses and Valuation

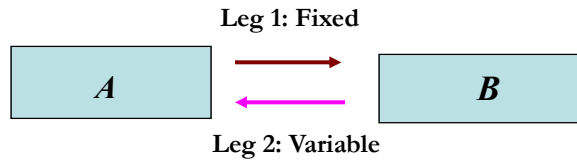
## SWAPS: Definition and Types

### Definition

A *swap* is a contract between two parties to deliver one sum of money against another sum of money at periodic intervals.

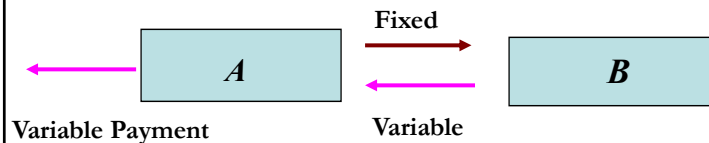
- Obviously, the sums exchanged should be **different**:
  - Different **amounts** (say, one fixed & the other variable)
  - Different **currencies** (say, USD vs EUR)
- The two payments are the *legs* or sides of the swap.
  - Usually, one leg is *fixed* and one leg is *floating* (a market price).
- The swap terms specify the duration and frequency of payments.

**Example:** Two parties (*A* & *B*) enter into a swap agreement. The agreement lasts for 3 years. The payments will be made semi-annually. Every six months, *A* and *B* will exchange payments.



- Swaps can be used to change the profile of a firm's cash flows.

If a swap is **combined** with an **underlying position**, one of the (or both) parties can change the profile of their cash flows (and risk exposure). For example, *A* can change its cash flows from variable to fixed.



### • Types

Popular swaps:

- Interest Rate Swap (one leg floats with market **interest rates**)
- Currency Swap (one leg in one **currency**, other leg in another)
- Equity Swap (one leg floats with market **equity returns**)
- Commodity Swap (one leg floats with market **commodity prices**)
- CDS (one leg is paid if **credit event occurs**)

Most common swap: **fixed-for-floating** interest rate swap.

- Payments are based on hypothetical quantities called *notionals*.
- The fixed rate is called the *swap coupon*.
- Usually, only the *interest differential* needs to be exchanged.

- Usually, one of the parties is a **Swap Dealer**, also called *Swap Bank*.

**Example:** Interest Rate Swap (inception date: April)

Bank Ardiles (**fixed-rate payer**) *buys* an 8% swap

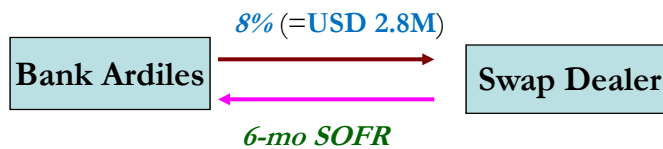
Notional: **USD 70M**

Swap coupon (Fixed-rate): **8% (s.a.)**.

Floating-rate: **6-mo. SOFR** (= Secured Overnight Financing Rate).

Payment frequency: semiannual (April and October).

Maturity = Swap term or Swap tenor = 3 years.



Every six months Bank Ardiles (fixed-rate payer) pays:

$$\text{USD } 70\text{M} * .08/2 = \text{USD } 2.8\text{M}$$

Every six months Swap Dealer (floating-rate payer) pays:

$$\text{USD } 70\text{M} * \text{6-mo SOFR}/2$$

**Example: (continuation)**

First payment exchange is in October. (The floating rate has already been fixed in April: **7.6%**.) Then, the Swap Dealer pays:

$$\Rightarrow \text{USD } 70\text{M} * .076/2 = \text{USD } 2.66\text{M}$$

Bank Ardiles (fixed-rate payer) pays **USD 0.14M** to the floating-rate payer:

$$\text{USD } 2.8\text{M} - \text{USD } 2.66\text{M} = \text{USD } 0.14\text{M}$$

Note: In October, the floating rate will be fixed for the second payment (in April of following year). ¶

## Market Organization

- Most swaps are tailor-made contracts.
  - Swaps trade in an **OTC** type environment.
  - **Swap specialists** fill the role of broker and/or market maker.
  - Brokers/market makers are usually **large banks**.
  - Prices are quoted with respect to a standard, or generic, swap.
- *All-in-cost*: Price of the swap (quoted as the rate the fixed-rate side will pay to the floating-rate side)
- It is quoted on a **semiannual basis** (s.a.):
  - absolute level ("9% fixed against six-month *SOFR flat*")
  - bp spread over the U.S. Treasury yield curve ("the Treasury yield plus **54 bps** against 6-mo *SOFR flat*").

"SOFR flat" = SOFR is quoted without a premium or discount.

- The fixed-rate payer is said to be "long" or to have "bought" the swap.

**Example:** Houseman Bank's *indicative swap pricing schedule*.

Maturity	HB Receives Fixed	HB Pays Fixed
1 year	1-yr TN sa + 44 bps	2-yr TN sa + 39 bps
2 years	2-yr TN sa + 50 bps	2-yr TN sa + 45 bps
3 years	<b>3-yr TN sa + 54 bps</b>	<b>3-yr TN sa + 48 bps</b>
4 years	4-yr TN sa + 55 bps	4-yr TN sa + 49 bps
5 years	5-yr TN sa + 60 bps	5-yr TN sa + 53 bps

- Consider the 3-year swap quote:

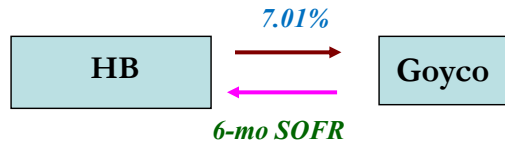
HB attempts to **sell** a 3- year swap to receive the offered spread of **54 bps** and **buy it back** to pay the bid spread of **48 bps**. HB's profit: **6 bps**.

**Example:** Goyco, a HB's client, wants to receive fixed-rate payments rather than pay fixed-rate for 3 years.

The current (“*on the run*”) 3-yr Treasury Note rate is **6.53%**.

Goyco enters into a 3-yr swap.

Calculation of fixed rate: HB will pay **7.01%** (**6.53** + **.48**) s.a. ¶



Note: SOFR will be reset at (T-2) for the next 6-mo period.

• Q: Are swaps riskless?

A: No! Default risk is always present.

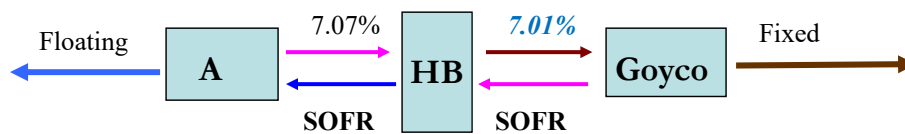
### • The Dealer's Perspective

A swap dealer intermediating (making a market in) swaps makes a living out of the spread between the two sides of the swap.

**Example:** Houseman Bank entered into a 3-year swap with Goyco.

3-year quote: 3-yr TN sa + **48 bps** & 3-yr TN sa + **54 bps**

The *on the run* 3-yr Treasury Note rate is **6.53%**.



HB finds a counterparty A  $\Rightarrow$  HB gets rid of the swap exposure. ¶

Note: The difference between the rate paid by the fixed-rate payer over the rate of the *on the run* Treasuries with the same maturity as the swap is called the **swap spread**. In this example, the swap spread is **54 bps**.

**Warehousing**

When the SD matches the two sides (the buyer and the seller) of a swap is called **back-to-back transaction**, or “**matched book**” transaction.

In practice, a SD may not be able to find an immediate off-setting swap.

Most SD will **warehouse** the swap and **use interest rate derivatives** to hedge their risk exposure until they can find an off-setting swap.

In practice, it is **not always possible to find a second swap** with the same maturity and notional principal as the first swap:

⇒ Swap dealers usually have a residual exposure.

The relatively narrow bid/ask spread in the interest rate swap market implies that to make a profit, effective interest rate risk management is essential.

**• Market Size**

Notional amount outstanding (Nov 2022):	<b>USD 463.0 trillion.</b>
- Interest rate swaps:	<b>USD 414.2 trillion</b>
- Currency swaps:	<b>USD 30.3 trillion (≈ 7%)</b>
- Equity-linked contracts (includes forwards):	<b>USD 6.9 trillion</b>
- Commodity contracts (includes forwards):	<b>USD 2.3 trillion</b>
- CDS market:	<b>USD 9.3 trillion (≈ 2%)</b>
- Gross market value:	<b>USD 16.35 trillion</b>

Interest rate swap is a very popular derivative: It represents **60%** of the Global OTC Derivatives Market.

Interest rate swaps also show big growth from early 1990s.

## Swaps: Why Use Them?

### • Using Swaps

- Manage risks (change profile of cash flows)
- Arbitrage (take advantage of price differentials)
- Enter new markets (firms can indirectly create new exposures)
- Create new instruments (no forward contract exist, a swap completes the market)

#### (1) Change profile of cash flow

Goyco's underlying situation: Fixed payments to bondholders, but wants floating debt.



Solution: A fixed-for-floating debt solves Goyco's problem.

**Example:** Goyco enters into a swap agreement with a Swap Dealer.

*Terms:*

Duration: 3-years.

Goyco makes floating payments (indexed by SOFR) and receives fixed payments from the Swap Dealer.



Q: Why would Goyco enter into this swap?

A: To **change the profile** of its cash flow: From fixed to floating. ¶

- Swaps are derivative instruments (derived valued from value of legs!).

## Interest Rate Swaps

- Most common swap: **fixed-for-floating** (*plain vanilla swap*)
  - Used to **change profile of cash flows** (a firm can go from paying floating debt to paying fixed debt).
  - Used to **lower debt costs**.
- Basis swap: floating-for-floating (*basis swaps*)
  - Floating rates should be **different**, say 1-mo **SONIA** vs. 3-mo SONIA (Sterling Overnight Index Average) or USD T-bill vs **SOFR**
  - Floating-for-floating currency swaps (also called **cross currency basis swaps**) are especial cases of interest rate basis swaps.
- Interest rates swaps have **very low** bid-ask spreads, lower than corporate bonds and, sometimes, government bonds.

### Example: Plain Vanilla Swap

Underlying situation for Ardiles:

- **USD 70 M** floating debt at: **6-mo SOFR + 1%**.
- Ardiles wants to change to fixed-rate USD debt.
- Currently, fixed-rate debt trades at **9.2%** (s.a.).

A Swap Dealer (Bertoni Bank) offers **8% (s.a)** against **6-mo SOFR**.

Terms: - Notional amount: **USD 70 M**

- Frequency: semi-annual
- Swap term or tenor (Duration): 4-years
- Fixed Coupon: **8% (s.a)**  $\Rightarrow$  **USD 70 M \* .08/2 = USD 2.8M**

Ardiles Co. and SD only exchange the **net payment** (difference between the two legs of the swap: Ardiles pays SD if 6-mo SOFR < **8%**).

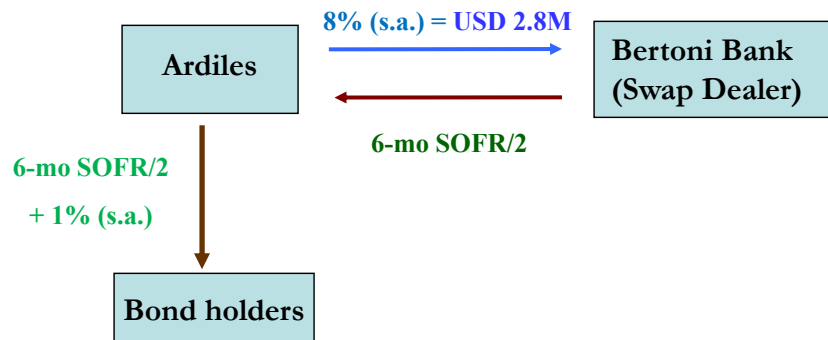
Notionals, obviously, will not be exchanged at maturity (year 4).

**Example (continuation):**

- Ardiles pays **8% (s.a.)** against **6-mo SOFR**.

Ardiles reduces its cost of borrowing to:

$$(\text{6-mo SOFR} + 1\%) + 8\% - \text{6-mo SOFR} = 9\% \text{ (s.a.) } (< 9.2\%)$$



Now, Ardiles has eliminated floating rate (**6-mo SOFR**) exposures. ¶

**Valuation of an Interest Rate Swap**

Assume **no** possibility of **default**. (Credit risk zero!)

- An interest rate swap can be valued:
  - As a **portfolio of bonds**: long position in one bond and a short position in another bond
  - As a **portfolio of forward contracts**.

- We will value a swap as a **portfolio of bonds**. Define:

V: Value of swap

$B_{\text{Fixed}}$ : NPV of fixed-rate bond underlying the swap

$B_{\text{Float}}$ : NPV of floating-rate bond underlying the swap

$$\Rightarrow \text{Value to the fixed-rate payer (Ardiles Co.)} = V = B_{\text{Float}} - B_{\text{Fixed}}$$

Note: At inception,  $V \approx 0$ . The swap has to be *fair*. That is, the fixed coupon is set in a way that the NPV of both sides is approximately equal.

- The discount rates should reflect the level of risk of the cash flows:  
An **appropriate discount rate** is given by the **floating-rate** underlying the swap agreement. In previous example, **6-mo. SOFR**.
- Since the discount rate is equal to the floating-rate payment, the value of the floating side payments ( $B_{\text{Float}}$ ) is equal to par value.  
 $\Rightarrow V$  changes when  $B_{\text{Fixed}}$  changes -the NPV of fixed-rate payments.
- If coupon (fixed-rate) payment is higher than discount rate, then:  
 $B_{\text{Fixed}} > B_{\text{Float}} \Rightarrow$  fixed-rate payer has a **negative** swap valuation ( $V < 0$ )

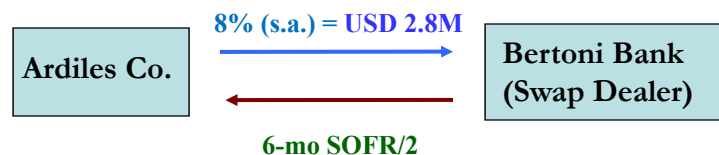
Technical Note: To use this approach to value a swap, we need to add an exchange of principals (in practice, it does not occur).

**Example:** Back to Ardiles' swap. Suppose the swap has **2 years left**.

Relevant SOFR rates: 6-mo: 6.00%; 12-mo: 6.25%; 18-mo: 6.25%; & 24-mo: 6.50%

Notional amount: **USD 70 M**

Ardiles pays **8%** (s.a.) fixed.



$$B_{\text{Fixed}} = \frac{2.8\text{M}}{[1 + .06 * (181/360)]} + \frac{2.8\text{M}}{[1 + .0625 * (365/360)]} + \frac{2.8\text{M}}{[1 + .0625 * (546/360)]} + \frac{72.8\text{M}}{[1 + .065 * (730/360)]} = \text{USD } 72,521,371.94$$

$$B_{\text{Float}} = \frac{2.1\text{M}}{[1 + .06 * (181/360)]} + \frac{2.1875\text{M}}{[1 + .0625 * (365/360)]} + \frac{2.1875\text{M}}{[1 + .0625 * (546/360)]} + \frac{72.275\text{M}}{[1 + .065 * (730/360)]} = \text{USD } 69,951,000.36 \quad (B_{\text{Float}} \approx Q. \text{ Why?})$$

**Example (continuation):** We used an **Actual/360** day count:

$$B_{\text{Fixed}} = \text{USD } 72,521,371.94$$

$$B_{\text{Float}} = \text{USD } 69,951,000.36$$

Value of the swap to Ardiles (the fixed-rate payer):

$$V = \text{USD } 69,951,000.36 - \text{USD } 72,521,371.94 = \text{USD } -2,570,368.38$$

Interpretation:

- Ardiles can **pay USD 2,570,368.38** the SD to close the swap.
- Alternatively, SD can **sell** the swap –i.e., the CF– for **USD 2,570,368.38**.

Note: Today, a similar swap, with  $T = 2$  years, would have a fixed coupon = **6.26% (s.a.)**; with a s.a. payment of **USD 2.191M**. Check:

$$\begin{aligned} B_{\text{Fixed}} &= 2.191\text{M}/[1 + .06*(181/360)] + 2.191\text{M}/[1 + .0625*(365/360)] + \\ &\quad + 2.191\text{M}/[1 + .0625*(546/360)] + 72.191\text{M}/[1 + .065*(730/360)] \\ &= \text{USD } 69,972,490 \quad \Rightarrow \text{At inception, } V \approx 0! \P \end{aligned}$$

## Currency Swaps

- Also called *Cross currency swaps* (XCCY).
- The legs of the swap are denominated in **different currencies**.
- Currency swaps change the **profile of cash flows**.
- Many possibilities for the CF exchanges: fixed-fixed, fixed-floating & floating-floating.
- Reference rates are **SOFR** & Ameribor (USD), **€STR** or Euro Short-Term Rate (EUR), **TONAR** (JPY), etc.

**Example:**

Situation: ExxonMobil has USD debt, but wants to increase EUR debt.

Solution: A swap.

ExxonMobil pays EUR. A Swap Dealer pays USD.

**Example (continuation):**

ExxonMobil pays EUR. A Swap Dealer pays USD.

- Swap Details:

- ExxonMobil pays **3.5%** in EUR, with a Notional principal: **EUR 20 M**
- Swap Dealer pays **4%** in USD, with a Notional principal **USD 26 M**
- Frequency of payments = 6-mo (**s.a.**)
- Duration = 4 years
- $S_t = 1.30$  USD/EUR.

Every six month, Exxon pays **EUR 350,000** & receives **USD 520,000**.

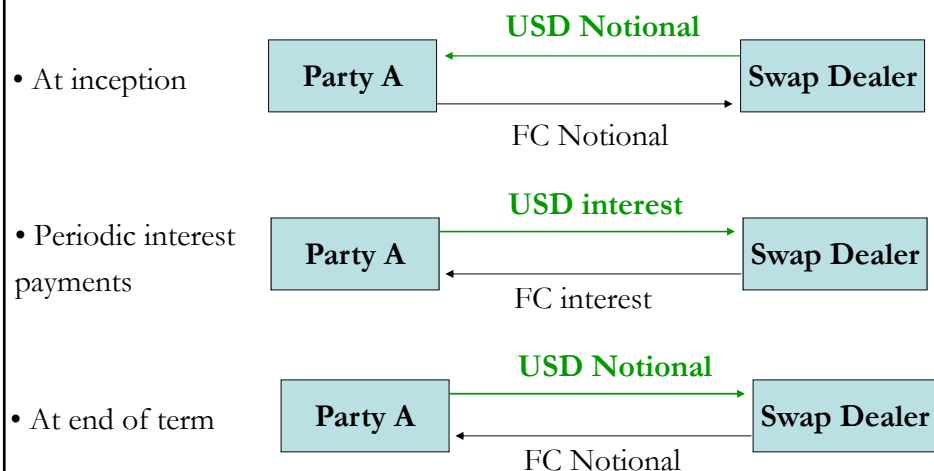


Note that Exxon and SD have implicitly fixed  $S_t$  for 4 years at:

$$S_{t+j} = \text{USD } 520,000 / \text{EUR } 350,000 = 1.485714 \text{ USD/EUR } \quad j=6,12,\dots,48. \quad \P$$

Usual CFs in a XCCY swap

In currency swaps the notional principals are **usually exchanged**. There are three sets of cash flows:



Note: Similar to an exchange of bonds. At inception, Party A receives USD “funding” and pays interest during the duration (“tenor”) of swap.

**Currency Swaps: Variations**

Key: Both legs are different currencies. **Different Instruments:**

1. Fixed-Fixed

**Example:** Exxon-Mobile example.

2. Fixed-Floating (also called *Circus swap* = Combined Interest Rate & Currency Swap)

**Example:** IBM pays 3-mo Ameribor in USD and receives 5% in EUR. ¶

3. Floating-Floating (also called *cross currency basis swap*, if initial exchange of notionals occurs)

**Example:** IBM pays 3-mo Ameribor in USD and receives 3-mo ESTR – **30 bps**. This EUR/USD XCCY swap is quoted “**-30 bps**.”

**Note:** **-30 bps** is the *spread* in EUR. The *spread* could be zero (IRP holds), positive or negative. ¶

**Valuation of Currency Swaps**

A currency swap can be decomposed into a position in two bonds:

- A domestic bond (or foreign currency 1 bond)
- A foreign bond (or foreign currency 2 bond)

**V** = Value of Swap (to DC payer) = NPV of FC bond – NPV of DC bond

In previous example the swap value to ExxonMobil is:

$$V = B_D - S_t B_F$$

$B_F$ : Value of FC denominated bond underlying the swap.

$B_D$ : Value of DC denominated bond underlying the swap.

$S_t$ : Spot exchange rate.

**Note:** For the Swap Dealer, the swap value (in DC) is:

$$V = S_t B_F - B_D$$

**Example FI:**

A U.S. financial institution (FI) is involved in a currency swap:

*Terms:*

- Frequency of payment: Annual.
- Notional principals: **DKK 53 million** & **USD 10 million**.
- FI get **5.5% p.a.** in DKK against **6% p.a.** in USD
- Payments: FI pays **USD 0.6M** & receives **DKK 2.915M**
- Swap will last for another three years ( $T = 3$  years).

$S_t = 0.18868$  **USD/DKK**.

Term structure in Denmark & U.S. is *flat*, with  $i_{DKK} = 5\%$  &  $i_{USA} = 6.5\%$ .



Note: At maturity, the principals will also be exchanged.

**Example FI (continuation):**

These periodic exchanges set an implicit forward contract (the swap forward rate), fixing  $S_t$  for each year at:

$$S_{t+j} = \text{USD } 0.6\text{M} / \text{DKK } 2.915\text{M} = 0.2058319 \text{ USD/DKK}, \quad j=1, 2, 3.$$

There are 3 *long* forward contract for FI:

Maturity ( $T$ ) = 1 year, 2 years, & 3 years.

Size: **DKK 2.915M**

Swap forward FX rate: **0.2058319 USD/DKK**

Note: Potentially, like in all long forward contracts, the FI profits if, at any  $T$ , the market forward rate,  $F_{t,t_j}$ , is higher than **0.2058319 USD/DKK**.

**Example FI (continuation):**

Discount rates:  $i_{DKK} = 5\%$  &  $i_{USA} = 6.5\%$ .

Coupons: **DKK 2.915M** & **USD 0.6M**

$T = 3$  years.

$S_t = 0.18868$  USD/DKK.



$$B_D = \frac{.6M}{(1+.065)} + \frac{.6M}{(1+.065)^2} + \frac{.6M}{(1+.065)^3} + \frac{10M}{(1+.065)^3} = \text{USD } 9,867,577$$

$$B_F = \frac{2.915M}{(1+.05)} + \frac{2.915M}{(1+.05)^2} + \frac{2.915M}{(1+.05)^3} + \frac{53M}{(1+.05)^3} = \text{DKK } 53,721,661$$

$$V_{US FI} = (53,721,661) * (.18868) - 9,867,577 = \text{USD } 268,585.45.$$

$$V_{SD} (\text{paying DKK and receiving USD}) = \text{USD } -268,585.45. ¶$$

Decomposition into Forward Contracts

The CFs of currency swap can be **valued** as a **series of forward contracts**, which are set by the exchanges of interest payments & principals.

Recall the value of a long forward contract is the present value of the amount by which the forward price exceeds the delivery price.

**Example FI (continuation):**

Annual exchanges: **DKK 2,915,000 = USD 600,000**

At maturity, final exchange: **DKK 53 M = USD 10 M**

⇒ Each of these payments represents an implicit forward contract.

- Swap forward rate fixed by the annual exchanges of interest payments:

$$\text{USD } 0.6M / \text{DKK } 2,915,000 = 0.2058319 \text{ USD/DKK.}$$

- Swap forward rate fixed by the last exchange of principals at  $T = 3$  years:

$$\text{USD } 10M / \text{DKK } 53M = 0.1886792 \text{ USD/DKK. ¶}$$

- We value the swap forward rate relative to the IRPT forward rate,  $F_{t,T}$ :

$$F_{t,T} = S_t * \frac{(1 + i_d * \frac{T}{360})}{(1 + i_f * \frac{T}{360})}$$

Suppose in the swap, we are long the FC (the FI is long DKK). Then, the PV, using  $i_d$  as the discount rate, of each annual payment  $j$  is:

$$(F_{t,t_j} - \text{Swap forward rate at time } t_j) * \frac{\text{Amount of FC}}{(1 + i_{d,j})^{t_j}}$$

#### Example FI (continuation):

FI's value of the exchange of principals at  $T = 3$  years ( $\text{Value}_{\text{FI,Principals}}$ ).

$$F_{t,T=3\text{-yr}} = .18868 \text{ USD/DKK} * \frac{(1 + .065)^3}{(1 + .05)^3} = .19688 \text{ USD/DKK}$$

Swap forward rate = USD 10M/DKK 53M = 0.1886792 USD/DKK.

$$\text{Value}_{\text{FI,Principals}} = (.19688 - 0.1886792) * \frac{53\text{M}}{(1 + .065)^3} = \text{USD } 0.35982\text{M}$$

Note: We can do the same for each exchange of CFs. ¶

- Alternatively, we can value the CFs in terms of forward DC.

Notation:

$t_j$ : time of the  $j$ th settlement date

$i_{d,j}$ : domestic interest rate applicable to time  $t_j$

$F_{t,t_j}$ : forward exchange rate applicable to time  $t_j$ , calculated by IRPT.

- PV to the FI of the swap forward contract set by the corresponding exchange of payments at time  $t_j$ :

$$(\text{DKK } 2,915,000 * F_{t,t_j} - \text{USD } 0.6\text{M}) * \frac{1}{(1 + i_{d,j})^{t_j}}$$

- PV to the FI of the swap forward contract set by the exchange of principal payments at time  $T$ :

$$(\text{DKK } 53\text{M} * F_{t,T} - \text{USD } 10\text{M}) * \frac{1}{(1 + i_{d,T})^T}$$

⇒ The value of a currency swap can be calculated from the term structure of forward rates and the term structure of  $i_{d,j}$ .

**Example (continuation):** Reconsider FI Example.

$$S_t = .18868 \text{ USD/DKK.}$$

$$i_{DKK} = 5\%$$

$$i_{USA} = 6.5\%.$$

Using IRPT, the one-, two- and three-year forward exchange rates are:

$$F_{t,T=1\text{-yr}} = .18868 \text{ USD/DKK} * \frac{(1 + .065)}{(1 + .05)} = .19137 \text{ USD/DKK}$$

$$F_{t,T=2\text{-yr}} = .18868 \text{ USD/DKK} * \frac{(1 + .065)^2}{(1 + .05)^2} = .19411 \text{ USD/DKK}$$

$$F_{t,T=3\text{-yr}} = .18868 \text{ USD/DKK} * \frac{(1 + .065)^3}{(1 + .05)^3} = .19688 \text{ USD/DKK}$$

**Example (continuation):** Reconsider FI Example.

- The value of the implicit swap forward contracts corresponding to the exchange of interest are therefore (in millions of USD):

$$(\text{DKK } 2.915 * .19137 \text{ USD/DKK} - \text{USD } .6) * \frac{1}{(1 + .065)} = \text{USD } -.03957\text{M}$$

$$(\text{DKK } 2.915 * .19411 \text{ USD/DKK} - \text{USD } .6) * \frac{1}{(1 + .065)^2} = \text{USD } -.03013\text{M}$$

$$(\text{DKK } 2.915 * .19688 \text{ USD/DKK} - \text{USD } .6) * \frac{1}{(1 + .065)^3} = \text{USD } -.02160\text{M}$$

- The final exchange of principal involves receiving **DKK 53M** & paying **USD 10M**. The value of the forward contract is:

$$(\text{DKK } 53\text{M} * .19688 \text{ USD/DKK} - \text{USD } 10\text{M}) * \frac{1}{(1 + .065)^3} = \text{USD } 359,816$$

- Then, the total value of the swap is (in USD):

$$359,816 - 39,570 - 30,130 - 21,600 = \text{USD } 268,516.$$

⇒ FI would be willing to sell this swap for **USD 268,516**. ¶

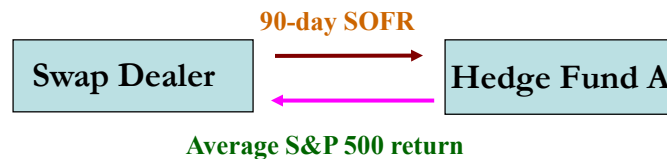
## Equity Swaps

Equity swaps have two legs: One of the legs is pegged to the return of a stock or market index. Usually, the other is pegged to a floating rate (SOFR or ESTR **plus or minus a spread**).

Terms include notional principal, duration and frequency of payments.

**Example:** Stock returns against a floating rate.

On April 1, Hedge Fund A enters into a 3-year equity swap. Every quarter, Hedge Fund A pays the **average S&P 500** return in exchange of **90-day SOFR** (count 30/360) .



**Example: (continuation)**

Notional principal = **USD 40 million**.

Data at inception (April 1):

S&P500 index = **4100**

90-day SOFR = **3%**.

On July 1, Hedge Fund A will pay (or receive if sum is negative):

**USD 40 M** \* [**S&P 500 return (04/01 to 07/01)** – **0.03** \* 90/360].

If on July 1, S&P 500 = **4153**  $\Rightarrow$  **Return** = **4153/4100** – 1 = **.0130**.

Then the payment will be:

**USD 40M** \* [**.0130** – **0.03** \* 90/360] = **USD 0.22M**.

On July 1, SOFR is set for the next 90-day period (07/01 to 10/01). ¶

### • Variations

- Equity return against a **fixed rate** (S&P500 against 2%)
- Equity return against **another equity return** (S&P500 against NASDAQ)
- Equity return against a **foreign equity return** (S&P500 against FTSE)
- Equity swaps **with changing notional** (“reinvested”) principals

### • Q: Why equity swaps?

- (1) Avoid **transaction costs** and **taxes**.
- (2) Avoid **legal limits** (margins, capital controls) and **institutional rules**.
- (3) Keep equity positions (and voting shares) **without equity risk**.

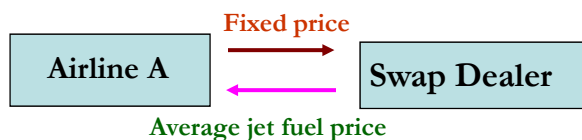
## Commodity Swaps

Commodity swaps work like any other swap: one leg involves a fixed commodity price and the other leg a (variable) commodity market price.

Unlike futures commodity contracts, *cash settlement* is the norm.

**Example:** Jet fuel oil swap.

Airline A enters into a 2-year jet-fuel oil swap. Every quarter, Airline A receives the **average market price** –based on a known price quote- & pays a **fixed price**.



**Example:** (continuation)

Cash settlement: If the average jet-fuel price paid is above (below) the fixed price, the SD will repay (receive from) the airline the difference in what it paid versus the fixed price. ¶

Note: There is no futures contract for jet fuel oil. A swap **completes** the **market**.

You can consider the 2-year swap as a **collection** of 8 **forward contracts**.

• **Q: Why commodity swaps?**

(1) *A commodity swap eliminates basis risk*

Southwest Airlines has used NYMEX crude oil and heating oil futures contracts to hedge jet fuel price risk. But, this introduces basis risk.

(2) *Expanded market*

Since there is cash settlement, market participants do not need to have the infrastructure to take delivery.

• **Commodity for interest swap**

They work like an equity swap: One leg pays a return on a commodity, the other leg pays an interest rate (say, SOFR plus or minus a spread).

**Example:** An oil producer enters into a 2-year swap. Every six month, the oil producer pays the **return on oil** –based on NYMEX Light Crude Oil– and receives **6-mo SOFR**.



• **Valuation of Commodity Swaps**

Commodity swaps are valued as a series of **commodity forwards**, each priced at inception with zero value.

The fixed coupon payment is a weighted average of commodity forward prices.

## Combination of Swaps

- Recall that swaps change the profile of cash flows.
- Swaps solve problems: *Financial Engineering*.

**Example:** A Brazilian oil producer is exposed to two forms of **price risk**:

- $P_{oil}$  (priced in USD/barrel of oil)  $\Rightarrow$  **Commodity price risk**.
- $S_t$  (BRL/USD)  $\Rightarrow$  **FX risk**.

Situation: Since expenses are in BRL, the Brazilian oil producer wants to **fix  $P_{oil}$  in BRL/barrel of oil**.

Solution: *Financial Engineering*, a combination of swaps can do it!

Note: This is a typical problem for commodity producers and buyers from non-USD zones: Commodities are priced in USD.

### Diagram: Structured Solution for Brazilian Oil Producer

