

## Chapter 3 Inventory Management

<b>3.1</b>	<b>Economic order quantity (EOQ)</b>	<b>22</b>
<b>3.2</b>	<b>EOQ with backorders (EOQBACK)</b>	<b>25</b>
<b>3.3</b>	<b>EOQ with quantity discounts (EOQDISC)</b>	<b>27</b>
<b>3.4</b>	<b>EOQ for production lot sizes (EOQPROD)</b>	<b>30</b>
<b>3.5</b>	<b>Reorder points and safety stocks (ROP)</b>	<b>32</b>

*The basic EOQ model in Section 3.1 finds that particular quantity to order which minimizes the total variable costs of inventory. The basic EOQ does not allow backorders; when backorders are possible, a modified EOQ model is available in EOQBACK. Another modification is found in EOQDISC, for cases where vendors offer price discounts based on the quantity purchased. If the EOQ is produced in-house rather than purchased from vendors, use the EOQPROD model. When demand is uncertain, the ROP worksheet computes reorder points and safety stocks to meet a variety of customer service goals. You must determine the order quantity before you can apply the ROP worksheet.*

### 3.1 Economic order quantity (EOQ)

The purpose of the EOQ model is simple, to find that particular quantity to order which minimizes the total variable costs of inventory. Total variable costs are usually computed on an annual basis and include two components, the costs of ordering and holding inventory. Annual ordering cost is the number of orders placed times the marginal or incremental cost incurred per order. This incremental cost includes several components: the costs of preparing the purchase order, paying the vendor's invoice, and inspecting and handling the material when it arrives. It is difficult to estimate these components precisely but a ball-park figure is good enough. The EOQ is not especially sensitive to errors in inputs.

The holding costs used in the EOQ should also be marginal in nature. Holding costs include insurance, taxes, and storage charges, such as depreciation or the cost of leasing a warehouse. You should also include the interest cost of the money tied up in inventory. Many companies also add a factor to the holding cost for the risk that inventory will spoil or become obsolete before it can be used. Annual holding costs are usually computed as a fraction of average inventory value. For example, a holding rate of .20 means that holding costs are 20% of average inventory. What is average inventory? A good estimate is half the order quantity. Here's the reasoning: when a new order arrives, we have the entire order quantity on hand. Just before the new order arrives, stocks are usually near zero. Thus the average inventory on hand is the average of the high point (the order quantity) and the low point (zero), or half the order quantity.

To see how the EOQ is computed, look at Figure 3-1, a template used by the Rebel Distillery in Shiloh, Tennessee. Each year the company requires 40 charred oak barrels for aging its fine sour-mash bourbon. A local supplier builds the barrels for Rebel and other distilleries in the area at a unit price of \$250. Rebel uses costs of \$25 per order and .125 for holding inventory. The EOQ is 8 units per order. If Rebel orders 8 units at a time, the total variable cost per year is minimized at \$250. You can prove that this is correct by using the table starting at row 23. If Rebel orders once per year, the order cost is \$25. Holding cost is \$625, computed as follows: The order size is 40 units and average inventory is 20 units. Then  $20 \times \$250 \times .125 = \$625$ . Total variable cost is  $\$25 + \$625 = \$650$ . Two orders per year result in  $2 \times \$25 = \$50$  in ordering cost. The order size is  $40/2 = 20$  and average inventory is 10 units. Then  $10 \times \$250 \times .125 = \$312.50$ . Total variable cost is  $\$50 + \$312.50 = \$362.50$ , and so on. The minimum occurs at 5 orders per year, the point at which total ordering and holding costs are equal. This is always true. Minimum total cost occurs when ordering and holding costs are equal.

**Figure 3-1**

	A	B	C	D	E	F	G	H	I
1	<b>EOQ.XLS</b>			<b>ECONOMIC ORDER QUANTITY</b>					
2									
3									
4	<b>HOLDING COST EXPRESSED AS RATE</b>					<b>HOLDING COST IN DOLLARS</b>			
5	INPUT:					INPUT:			
6	Annual usage in units			<b>40</b>		Annual usage in units			<b>40</b>
7	Unit price			<b>\$250.00</b>					
8	Cost per order			<b>\$25.00</b>		Cost per order			<b>\$25.00</b>
9	Holding rate			<b>0.125</b>		Annual holding cost per unit			<b>\$31.25</b>
10	Working days per year			<b>250</b>		Working days per year			<b>250</b>
11	OUTPUT:					OUTPUT:			
12	Total dollar value used per year			\$10,000.00					
13	Number of orders per year			5		Number of orders per year			5
14	Total ordering cost per year			\$125.00		Total ordering cost per year			\$125.00
15	Total holding cost per year			\$125.00		Total holding cost per year			\$125.00
16	Total variable cost per year			\$250.00		Total variable cost per year			\$250.00
17	Average inventory investment \$			\$1,000.00		Average inventory investment units			4
18	Number of days supply per order			50		Number of days supply per order			50
19	EOQ in units of stock			8		EOQ in units of stock			8
20	EOQ in dollars			\$2,000.00					
21									
22									
23	Nbr orders	Order cost	Holding cost	Total var cost					
24	1	\$25.00	\$625.00	\$650.00					
25	2	\$50.00	\$312.50	\$362.50					
26	3	\$75.00	\$208.33	\$283.33					
27	4	\$100.00	\$156.25	\$256.25					
28	5	\$125.00	\$125.00	\$250.00					
29	6	\$150.00	\$104.17	\$254.17					
30	7	\$175.00	\$89.29	\$264.29					
31	8	\$200.00	\$78.13	\$278.13					
32	9	\$225.00	\$69.44	\$294.44					
33	10	\$250.00	\$62.50	\$312.50					

Here is a quick summary of how to interpret the output cells. Total dollar value used per year is annual usage in units times the unit price. The number of orders is the annual usage in units divided by the EOQ. Total ordering cost is number of orders times cost per order. Total holding cost is average investment times the holding rate. Average investment is half the EOQ times the unit price. Number of days supply per order is 250 divided by the number of orders. The EOQ, or number of units per order is the standard formula:

$$\text{EOQ} = [(2 \times \text{annual usage} \times \text{cost per order}) / (\text{unit price} \times \text{holding rate})]^{1/2}$$

Why don't we include the purchase cost of the inventory in this calculation? It is not a variable cost. We have to purchase the inventory in any event. The problem is to minimize those costs that vary with the quantity purchased at one time.

If you are uncertain about the input values to the EOQ, do sensitivity analysis by using a range of different values. For example, at Rebel, management felt that the actual order cost was somewhere in the range of \$20 to \$30. This gives a range of order quantities from 7 to 9 units, so the 8-unit EOQ looks reasonable. Rebel was also concerned about the holding rate. Estimates in the range of .10 to .15 were tested, using an order cost of \$25. Again, the EOQ varied in the range 7 to 9 units. Click on the graph tab in the EOQ workbook for another view of cost sensitivity. The graph shows variable costs versus the number of orders placed per year. The total cost curve is relatively flat in the region of the EOQ (5 orders per year).

When the holding cost is expressed as dollars per unit per year rather a rate, an alternative model is available for computing the EOQ (columns F – I in Figure 3-1). Note that the unit price is not necessary in this alternative model.

### 3.2 EOQ with backorders (EOQBACK)

Backorders are common in inventories held for resale to customers. The EOQ model can be modified to handle backorders by including one more cost, the cost per unit backordered. This cost is extremely difficult to assess. In theory, the backorder cost should include any special cost of handling the backorder, such as the use of premium transportation, and any cost associated with loss of customer goodwill. As a surrogate for the true backorder cost, most companies use the profit per unit.

The backorder model has been employed for some time by the Ryan Expressway Nissan dealership in Freeport, Texas. Figure 3-2 is an analysis of inventory policy for the Nissan Maxima SE, which costs Ryan \$17,400. Ryan sells about 120 SEs per year. Order cost (primarily transportation) is \$225 per unit. Ryan's holding rate is .1875 of average inventory value. As a backorder cost, Ryan uses profit per unit, which averages \$730. The model tells Ryan to order an EOQ of 9.51 or about 10 cars. Backorders build up to about 7.77 cars by the time each EOQ arrives, and the average number on backorder during the order cycle is 3.18. Total variable cost is \$5,675.59.

The formula for the EOQ with backorders is:

$$\text{EOQ with backorders} = \left\{ \frac{(2 \times \text{annual usage} \times \text{cost per order})}{(\text{holding cost})} \times \frac{1}{[(\text{holding cost} + \text{backorder cost})/(\text{backorder cost})]} \right\}^{1/2}$$

The holding cost is unit price times the holding rate. Note that the square root is taken for the entire quantity inside the curly brackets.

In the worksheet, enter a backorder cost of zero for an EOQ of 4.07, with total costs of \$13,273.09. This is the same result as the standard EOQ model. Now, enter the backorder cost of \$730. This increases the EOQ to 9.51, and total costs are reduced to \$5,675.59.

Why did total costs go down? The last term in the equation above forces the backorder model to yield a smaller order quantity and therefore a smaller average inventory than the standard EOQ. In this example, average inventory goes down to almost nothing (0.16 cars) because as soon as the EOQ arrives, we use most of it to fill backorders. Of the 9.51 cars in the EOQ, 7.77 go to fill backorders, leaving less than two cars in stock.

The backorder model works well for Ryan because financing the inventory is so expensive. It is much less expensive to incur backorders and fill them when the EOQ arrives than it is to hold inventory. Of course, this is a risky policy and the backorder model must be used with caution. The model assumes that customers are willing to wait on backorders and are not lost to the company. If customers are lost, then the model is inappropriate. There are other models that account for lost customers but they are rarely used in practice because of the risks involved.

**Figure 3-2**

	A	B	C	D	E
1	<b>EOQBACK.XLS</b>	<b>EOQ WITH BACKORDERS</b>			
2					
3					
4	<b>HOLDING COST EXPRESSED AS RATE</b>			<b>HOLDING COST IN DOLLARS</b>	
5	<b>INPUT:</b>			<b>INPUT:</b>	
6	Annual usage in units	<b>120</b>		Annual usage in units	<b>120</b>
7	Unit price	<b>\$17,400.00</b>			
8	Cost per order	<b>\$225.00</b>		Cost per order	<b>\$225.00</b>
9	Holding rate	<b>0.1875</b>		Annual holding cost per unit	<b>\$3,262.50</b>
10	Backorder cost per unit	<b>\$730.00</b>		Backorder cost per unit	<b>\$730.00</b>
11	Working days per year	<b>300</b>		Working days per year	<b>300</b>
12	<b>OUTPUT:</b>			<b>OUTPUT:</b>	
13	Order quantities:			Order quantities:	
14	EOQ in units	9.51		EOQ in units	9.51
15	Number of days supply per order	23.79		Number of days supply per order	23.79
16	EOQ in dollars per order	\$165,551.04			
17	Backorder cost:			Backorder cost:	
18	No. of units backordered when the EOQ arrives	7.77		No. of units backordered when the EOQ arrive	7.77
19	Average units backordered	3.18		Average units backordered	3.18
20	Annual backorder cost	\$2,318.93		Annual backorder cost	\$2,318.93
21	Ordering cost:			Ordering cost:	
22	No. of orders per year	12.61		No. of orders per year	12.61
23	Annual ordering cost with backorders	\$2,837.80		Annual ordering cost with backorders	\$2,837.80
24	Holding cost:			Holding cost:	
25	Average inventory	0.16		Average inventory	0.16
26	Annual holding cost with backorders	\$518.87		Annual holding cost with backorders	\$518.87
27	Total annual cost:			Total annual cost:	
28	Backorder cost + ordering cost + holding cost	\$5,675.59		Backorder cost + ordering cost + holding cost	\$5,675.59

Some companies refuse to accept the idea that any specific cost is incurred for backorders. However, these companies still use the model in Figure 3-2 as a means of determining the EOQ that will yield some target number of backorders. This is done by treating the backorder cost as a control knob. We turn the knob until the target number of backorders is reached. In Ryan's case, what backorder cost should be employed to have only 2 cars on backorder when the EOQ arrives? The answer is \$5,200. Enter this value in the model and you get 2 cars on backorder, with an EOQ of 5.19. This represents about a 13-day supply of cars, compared to about 24 days with a backorder cost of \$730.

If holding costs are stated in dollar terms use the alternate model in Figure 3-2. You can repeat this example using a holding cost of \$3,262.50, which is the holding rate of .1875 x the unit price of \$17,400.

### **3.3 EOQ with quantity discounts (EOQDISC)**

Many companies blindly purchase in large quantities to get discount prices without considering all the tradeoffs involved. The costs may well outweigh any savings in purchase price. The EOQDISC model helps you analyze quantity discount offers and make better purchasing decisions.

In Figure 3-3, the Bellaire Printing Company in Bellaire, Texas, uses 1,000 drums of binding glue per year. Up to 499 drums can be purchased at a price of \$50 per drum. For 500 or more drums the price is \$48. At first glance, this is a good deal because savings in purchase costs are \$2,000 per year (1,000 drums x \$2 discount). But when total costs are considered, the discount plan costs the company more.

EOQDISC first computes the economic order quantity at standard price. This is shown in cell B11 and rounded up to the nearest integer in cell B12. Next, the model computes the holding cost of the inventory. The dollar value of an order is computed in cell B14. Just after an order is received the entire order is on hand. When all stock is consumed, inventory is zero. Thus average inventory on hand is estimated at half the order value. The annual holding cost is the holding rate times average inventory or \$463.75.

Another cost is associated with purchasing the item. The number of orders per year is 18.87, obtained by dividing the annual usage by the order quantity. It costs \$25 to process an order, so the annual purchasing cost is  $18.87 \times \$25 = \$471.70$ . The final cost is for the item itself. Multiplying the unit price times the annual usage yields \$50,000.00. Finally, the sum of holding, purchasing, and item costs is \$50,935.45.

**Figure 3-3**

	A	B	C	D	E	F
1	<b>EOQDISC.XLS</b>	<b>EOQ WITH QUANTITY DISCOUNTS</b>				
2						
3		<b>Standard</b>	<b>Discount</b>	<b>Discount</b>	<b>Discount</b>	<b>Discount</b>
4	<b>INPUT:</b>	<b>price</b>	<b>plan 1</b>	<b>plan 2</b>	<b>plan 3</b>	<b>plan 4</b>
5	Annual usage in units	1,000	1,000	1,000	1,000	1,000
6	Unit price	\$50.00	\$48.00	#N/A	#N/A	#N/A
7	Cost per order	\$25.00	\$25.00	\$25.00	\$25.00	\$25.00
8	Holding rate	0.3500	0.3500	0.3500	0.3500	0.3500
9	Min. order qty. to get discount	0	500	#N/A	#N/A	#N/A
10	<b>OUTPUT:</b>					
11	Trial order quantity	53.45	54.55	#N/A	#N/A	#N/A
12	Final order quantity	53	500	#N/A	#N/A	#N/A
13	Holding cost:					
14	Dollars in one order	\$2,650.00	\$24,000.00	#N/A	#N/A	#N/A
15	Average inventory in dollars	\$1,325.00	\$12,000.00	#N/A	#N/A	#N/A
16	Annual carrying cost	\$463.75	\$4,200.00	#N/A	#N/A	#N/A
17	Purchasing cost:					
18	Number of orders per year	18.87	2.00	#N/A	#N/A	#N/A
19	Annual purchasing cost	\$471.70	\$50.00	#N/A	#N/A	#N/A
20	Cost of the inventory item:	\$50,000.00	\$48,000.00	#N/A	#N/A	#N/A
21	Total cost per year:	\$50,935.45	\$52,250.00	#N/A	#N/A	#N/A



The same analysis is performed for the discount plan in column C. The trial EOQ turns out to be 54.55 units, too small to get the discount, so the order quantity is rounded up to the minimum that must be purchased. The result is a total cost of \$52,250, about 2.5% more than the total cost at standard price.

Now let's do some sensitivity analysis. Suppose that you are uncertain about the cost per order. Try a cost per order of \$50 and see what happens. You get annual costs of \$51,322.89 at the standard price and \$52,300 at the discount price. Now try an ordering cost of \$10. The costs are \$50,591.62 at the standard price and \$52,220 at the discount price. Thus, even if the ordering cost is wrong by a wide margin, you should not take this discount. You may also be uncertain about the annual usage or the holding cost per dollar. Again, sensitivity analysis of these factors is easy to do.

If you are in a position to bargain with the vendor on prices, use EOQDISC to find the breakeven price. This is the price at which you are indifferent about taking the discount because the annual costs for the standard price and the discount price are the same. You can use the breakeven price as the starting point for negotiating a better discount plan, one that benefits both vendor and customer. A little experimenting with EOQDISC shows that \$46.79 (a 6.4% discount) is the breakeven price. If you want to check this result, don't forget to reset the ordering cost to \$25. With this discount, total costs are about the same for both standard and discount prices.

Vendors sometimes offer several different price/quantity plans, so EOQDISC is set up to evaluate four discount plans at once. To analyze a new problem, the first step is to make new entries in the input data cells in column B for the standard price plan. Data for annual usage, cost per order, and holding rate are common to all plans, so formulas automatically repeat this information in columns C - F. Now enter unit prices and minimum order quantities. When data entry is complete, the total cost per year is automatically displayed in row 21.

EOQDISC requires input of the holding rate rather than holding cost in dollars. You can convert to a holding rate by dividing the holding cost in dollars by the unit price.

### 3.4 EOQ for production lot sizes (EOQPROD)

Alvin Air Systems in Alvin, Texas, produces repair and maintenance items for commercial air conditioning systems. Alvin cannot use the standard EOQ for determining production lot sizes. One problem is that the standard EOQ assumes that an order quantity or lot of material is received all at once. At Alvin, most production lots take some time to complete and parts are placed in stock on a daily basis until the run is over. A related problem is that substantial sales usually occur before the run is over. To solve these problems, Alvin uses the modified EOQ model in Figure 3-4. The data are for a rubber seal used in water pumps. Usage (sales) is 5,000 units per year at a price of \$8.00 each. Setup cost, the cost of cleaning supplies and the labor time to prepare the equipment, is \$125 per run. Alvin uses a holding rate of .20. Sales occur at an average rate of 20 units per day, while 100 units per day are produced. The output section shows that maximum investment is \$6,324.56 but the EOQ in dollars is \$7,905.69. Why? The EOQ must be larger than maximum investment to account for sales made during the production run. The formula for the EOQ with production lot sizes is:

$$\text{EOQ for production lots} = \frac{\{2 \times \text{annual usage} \times \text{cost per order}\}}{[(\text{unit price} \times \text{holding rate}) \times (1 - \text{sales rate}/\text{production rate})]}^{1/2}$$

The formula is the same as the standard EOQ except that the denominator of the fraction includes the term (1 - sales rate / production rate). This term inflates the EOQ to account for sales during the production run.

**Figure 3-4**

	A	B	C	D	E	F	G
1	<b>EOQPROD.XLS</b>	<b>EOQ FOR PRODUCTION LOT SIZES</b>					
2							
3	<b>HOLDING COST EXPRESSED AS RATE</b>			<b>HOLDING COST IN DOLLARS</b>			
4	INPUT:			INPUT:			
5	Annual usage in units	<b>5,000</b>		Annual usage in units			<b>5,000</b>
6	Unit price	<b>\$8.00</b>		Annual holding cost per unit			<b>\$1.60</b>
7	Setup cost per run	<b>\$125.00</b>		Setup cost per run			<b>\$125.00</b>
8	Holding rate	<b>0.20</b>					
9	Sales rate in units per day	<b>20</b>		Sales rate in units per day			<b>20</b>
10	Production rate in units per day	<b>100</b>		Production rate in units per day			<b>100</b>
11	Working days per year	<b>250</b>		Working days per year			<b>250</b>
12	OUTPUT:			OUTPUT:			
13	Total dollar value used per year	\$40,000.00					
14	Number of production runs per year	5.06		Number of production runs per year			5.06
15	Total ordering cost per year	\$632.46		Total ordering cost per year			\$632.46
16	Total holding cost per year	\$632.46		Total holding cost per year			\$632.46
17	Total variable cost per year	\$1,264.91		Total variable cost per year			\$1,264.91
18	Average inventory investment	\$3,162.28		Average inventory investment (units of stock)			395.28
19	Maximum inventory investment	\$6,324.56		Maximum inventory investment (units of stock)			790.57
20	Number of days supply per run	49.41		Number of days supply per run			49.41
21	Number of days required to produce EOQ	9.88		Number of days required to produce EOQ			9.88
22	Number of units per run (EOQ)	988.21		Number of units per run (EOQ)			988.21
23	Number of dollars per run (EOQ\$)	\$7,905.69					

### 3.5 Reorder points and safety stocks (ROP)

When demand is uncertain, inventory investment from the EOQ model should be supplemented with safety stock. ROP (Figure 3-5) is a worksheet used to compute safety stocks and reorder points (ROPs) at Channelview Inspection Company, a Houston-area firm that performs a variety of inspection, testing, and cleaning operations on pipe destined for use in oil and gas fields. The ROP model helps manage the maintenance parts and supplies used in this work. Look first at Part A. The data are for wire brushes used to clean the interior of pipe joints. Since work is delayed when brushes are out of stock, management wants no more than a 10% probability of shortage. About 2,000 brushes are used per year. The EOQ, or order quantity, is 200 units and leadtime demand averages 166.7 units. Since the volume of pipe received from customers varies, there is variation in leadtime demand, with a standard deviation of 60 units. Leadtime is 1 month and the length of the forecast interval (the time period covered by the forecast) is also 1 month.

When the stock of brushes falls to a certain level, called the reorder point, or ROP, we should reorder the EOQ of 200 units. This level should cover expected leadtime demand plus enough safety stock to give a 10% chance of shortage before the order arrives. The ROP is 243.6 units in cell D21. Let's work through the input and output cells to see how this value is determined. First, leadtime demand is defined as the total inventory usage expected to occur during a stock replenishment cycle. This cycle is measured from the time the replenishment order is released until it is received. The standard deviation is a measure of variation in leadtime demand. If there is no variation, the standard deviation is zero. As the standard deviation increases, demand becomes more uncertain, and we need more safety stock.

The standard deviation of leadtime demand may be known or it may have to be estimated from a forecasting model. The square root of the MSE of the forecast errors from one of the smoothing models in Chapter 2 is an approximate standard deviation of leadtime demand if leadtime is one time unit (week, month, or quarter). That is, the MSE in the smoothing models is always computed for 1-step-ahead forecasts. When the number of time periods in leadtime and the number of periods used to compute the standard deviation do not match, the standard deviation must be adjusted. This is done in cell D18 by multiplying the standard deviation by the square root of  $(D13/D14)$  or  $(\text{periods in leadtime})/(\text{periods used in standard deviation})$ .

Now we need to determine the number of adjusted standard deviations that should be used in safety stock. Cell D19 contains a formula that is equivalent to a table lookup from the normal distribution. This cell uses the probability in cell D8 to determine the number of standard deviations (often called a Z-score) needed to meet that probability target. Safety stock in cell D20 is the number of standard deviations times the size of the adjusted standard deviation. The ROP in D21 is the level of stock at which a new order is placed: the sum of leadtime demand plus safety stock.

Figure 3-5

	A	B	C	D	E	F	G	H	I
1	ROP.XLS		REORDER POINT (ROP) CALCULATOR						
2									
3		PART A:					PART B:		
4	What ROP will meet a target					What ROP will meet a target			
5	probability of shortage?					number of annual shortages?			
6									
7	INPUT:					INPUT:			
8	Probability of shortage			10.0%		No. of annual shortages			1.0
9	Annual demand			2,000.00		Annual demand			2,000.00
10	Order quantity			200.00		Order quantity			200.00
11	Demand during leadtime			166.70		Demand during leadtime			166.70
12	Std. dev. value			60.00		Std. dev. value			60.00
13	No. periods in leadtime			1.0		No. periods in leadtime			1.0
14	No. periods of demand			1.0		No. periods of demand			1.0
15	used to compute std. dev.					used to compute std. dev.			
16									
17	OUTPUT:					OUTPUT:			
18	Adjusted std. dev. value			60.0		Adjusted std. dev. value			60.0
19	No. of std. devs. (Z)			1.3		No. of std. devs. (Z)			1.3
20	Safety stock			76.9		Safety stock			76.9
21	ROP			243.6		ROP			243.6
22									
23	No. of annual orders			10.0		No. of annual orders			10.0
24	No. of annual shortages			1.0		No. of annual shortages			1.0
25	Average investment			176.9		Average investment			176.9
26	Maximum investment			276.9		Maximum investment			276.9
27	% ann. sales backordered			1.4%		% ann. sales backordered			1.4%
28						Probability of shortage			10.0%
29									
30									
31		PART C:					PART D:		
32	What shortage values result					What ROP will meet a target %			
33	from a given safety stock?					of annual sales backordered?			
34									
35	INPUT:					INPUT:			
36	Safety stock			76.9		% sales backordered			1.4%
37	Annual demand			2,000.00		Annual demand			2,000.00
38	Order quantity			200.00		Order quantity			200.00
39	Demand during leadtime			166.70		Demand during leadtime			166.70
40	Std. dev. value			60.00		Std. dev. value			60.00
41	No. periods in leadtime			1.0		No. periods in leadtime			1.0
42	No. periods of demand			1.0		No. periods of demand			1.0
43	used to compute std. dev.					used to compute std. dev.			
44									
45	OUTPUT:					OUTPUT:			
46	Adjusted std. dev. value			60.0		Adjusted std. dev. value			60.0
47	No. of std. devs. (Z)			1.3		No. of std. devs. (Z)			1.3
48	Safety stock			76.9		Safety stock			76.9
49	ROP			243.6		ROP			243.6
50									
51	No. of annual orders			10.0		No. of annual orders			10.0
52	No. of annual shortages			1.0		No. of annual shortages			1.0
53	Average investment			176.9		Average investment			176.9
54	Maximum investment			276.9		Maximum investment			276.9
55	% ann. sales backordered			1.4%		% ann. sales backordered			1.4%
56	Probability of shortage			10.0%		Probability of shortage			10.0%
57									

Given this ROP, we can compute several measures of performance for the inventory of brushes. There are 10 orders per year (annual demand divided by the size of the order quantity). This is also the number of leadtimes each year, so 10 leadtimes times a 10% probability of shortage on 1 leadtime equals 1 expected shortage per year in cell D24. Average inventory investment in D25 includes two components: half the order quantity plus all of the safety stock. The reasoning for counting half the order quantity in average investment is explained in section 3.1. Why do we count all of the safety stock? Sometimes demand will be less than expected and we will have safety stock left over following a leadtime. Sometimes demand will be greater than expected and we will use up all safety stock. So we count all of the safety stock in average inventory investment. The maximum inventory investment that should be on hand at one time occurs just after an order is received. The maximum is the sum of order quantity plus safety stock. Finally, cell D27 indicates that about 1.4% of annual sales units will be on backorder at any given time.

Part B of the model is similar to Part A except that the management goal is stated in terms of the number of shortages per year. When the items in an inventory are ordered different numbers of times each year, Part B can be used to assign safety stocks such that each item runs out of stock the same number of times. For example, suppose that one item is ordered 10 times per year and another is ordered 30 times. If each has a 10% probability of shortage, the first item will run out of stock once per year and the second will run out 3 times. You can use Part B to assign safety stocks so that each item has the same number of shortages. Part C is used when you want to check the shortage protection provided by some predetermined level of safety stock. Part D is used when you want to meet a goal for the percentage of annual sales backordered.

To solve your own problem in the ROP model, replace the input cells with your own entries. One potential complication is that some companies compute the MAD of the forecast errors rather than the standard deviation. For the normal distribution, the standard deviation is approximated by 1.25 times the MAD. Multiply the MAD by 1.25, enter the result as the standard deviation, and you can use the ROP worksheet as is. Another complication is that it is possible to meet a goal for the percentage of sales backordered using "negative safety stocks," by purposely running out of stock. Negative safety stocks are impractical in my opinion and the formulas in ROP do not work with them. If negative safety stocks occur in ROP, treat the results as an indication of an error in your input data.

## Exercises

- 3-1** Art Howe manages the pro shop at the Bayou Rifles Shooting Range in Juliff, Texas. Art's sales of Federal Classic High-Velocity .22 caliber ammunition are about \$220,000 per year. It costs \$30 to place an order and carrying cost is 18 percent. How many orders per year should Art place for .22 ammo?
- 3-2** Art needs to determine an optimal ordering policy for Comp-Tac Kydex holsters for the Browning Hi-Power in 9MM. Annual demand for the holsters is \$28,000. Carrying cost is 23 percent while order costs are \$48 per order. What are the optimal dollars per order?
- 3-3** Astro players use \$96,000 annually of mustache wax (provided by the team). Mike Scott, the purchasing director, estimates the ordering cost at \$45 and thinks that the team can hold this type of inventory at an annual storage cost of 22 percent of the purchase price. How many months of supply should Mike order at one time to minimize total annual cost of purchasing and carrying?
- 3-4** Cruz Chemical Company holds its inventory of raw material in special containers, with each container occupying 10 square feet of floor space. There are only 5,000 square feet of storage space available. Each year, Cruz uses 9,000 containers of raw material, paying \$8 per container. If ordering costs for raw material are \$40 per order and annual holding costs are 20 percent of the average inventory value, how much is it worth to Cruz to increase its raw material storage area? How many days' supply of inventory can be stored with the 5,000 square feet storage limitation, assuming Cruz works a 300-day year?
- 3-5** Prior to this year, Leo Durocher has ordered microwave ovens for his restaurant supply company according to the EOQ. He places 9.3 orders per year. Carrying and ordering costs are 30 percent and \$46 per order, respectively. Next year, annual demand for microwave ovens is expected to increase by 20 percent. How many orders will Leo place next year?
- 3-6** You have been retained as a consultant by Bagwell Bar-B-Q Grills, which maintains inventories of 10 items used in its manufacturing and assembly process. The company is not able

to determine its carrying cost or ordering cost with sufficient reliability to support the use of formal EOQ approaches, but it is nevertheless concerned that it is not managing its inventory as effectively as it might. These data concerning use and purchase of the 10 inventory items are available from last year's records:

<u>Item</u>	<u>Dollars used annually</u>	<u>No. purchase orders placed last year</u>
A	120,000	5
B	80,000	6
C	50,000	6
D	24,000	4
E	10,500	8
F	5,200	6
G	2,400	7
H	1,100	8
I	900	6
J	300	6

Using the data available, answer these questions:

- a. Without increasing the purchasing workload, what percentage reduction can you make in the average dollar inventory carried?
- b. If the company is willing to increase the purchasing workload by 25 percent, what is the minimum average inventory it can achieve?
- c. If the company is willing to increase its average inventory by 10 percent, what percentage reduction in purchasing workload can it achieve?

**3-7** Flash Gordon Footwear makes high-quality hiking and walking boots and shoes. Its heavy winter boot is made with a leather upper, a heavy vinyl sole, a nylon lining, and leather laces. Flash's walking shoe uses a leather upper, a rubber sole, and cloth laces. Materials are ordered every 6 months except the leather for uppers, which is ordered every 3 months. Yearly usage of materials is forecast to be follows: leather, \$200,000; vinyl soles, \$40,000; rubber soles, \$30,000; nylon lining, \$30,000; leather laces, \$4,000; cloth laces, \$2,000. What minimum average inventory can Flash achieve without adding to his purchasing workload?

**3-8** The Slusarski Outboard Motor Company has determined that the cost of being stocked out of motors is \$200 for each unit. An EOQ analysis indicates that the company should reorder 10 times each year. Carrying costs are \$20 per motor. Slusarski is considering dropping the



reorder point from 250 to 220. Based on the information in the table below, what would you advise the company to do?

<u>Usage during reorder period</u>	<u>Probability of this usage</u>
200	.10
220	.08
240	.06
260	.04
280	.02

**3-9** Given the following data for an SKU used by the Bottenfield Company (assume a 250-day work year), compute the reorder point:

EOQ	100
Average use per day	4 units
Average reorder period	25 days
Cost to store 1 unit per year	\$5
Cost of being out of stock per unit per time	\$20

<u>Usage during reorder period</u>	<u>Probability of this usage</u>
25	.05
50	.10
75	.15
100	.25
125	.20
150	.15
175	.10

**3-10** Drayton's Muffler Repair advertises that it is able to replace a car muffler on the same day a customer brings a car into the shop. If for any reason Drayton cannot keep this promise, he pays the customer \$100. Drayton has found that for LN-70 mufflers, the optimal reorder quantity is 30 mufflers; he orders LN-70 mufflers 10 times a year. As LN-70 mufflers have to be ordered from a manufacturer located a considerable distance away, lead time for his orders is 30 working days, a period of time in which Drayton on the average sells 30 LN-70 mufflers. During the past 10 years, 100 orders were placed. There were 10 occasions when Drayton sold 32 LN-70s, 5 occasions when he sold 35, and only 1 when he sold 36 during the 30-day order period. On each of the other 84 occasions, he sold 30 or fewer. If it costs Drayton \$18 a year to hold one LN-70 in safety stock, what should Drayton establish as his reorder point for LN-70 mufflers to minimize his costs? At this level of safety stock, how many \$100 bills will Drayton expect to give to car owners whose cars require an LN-70 muffler?

**3-11** Preston Gomez Distributing Company has maintained an ordering policy for power lawn mowers which allows for an 80 percent service level. Mean demand during the reorder period is 130 lawn mowers, and the standard deviation is 80 mowers. The annual cost of carrying one mower in inventory is \$6. The area salesperson have recently told Gomez management that they could expect a \$500 improvement in profit (based on current figures of cost per lawn mower) if the service level were increased to 99 percent. Is it worthwhile for Gomez to make this change?

**3-12** Hatton Manufacturing Company experiences a mean usage of 160 motor castings during the reorder lead time. The standard deviation of usage during this period is 26 castings. If the usage is normally distributed, what percentage of the time will Hatton experience stockouts if it maintains a safety stock of 24 castings?

**3-13** Bill Virdon's Sports Computer Shop stocks a very popular game called Astro Rally. Recently, some of the customers have complained about excessive stockouts and Bill is considering an increase in safety stock for the games. Bill has estimated that the demand during reorder lead time for Astro Rally is normally distributed with a mean of 50 games and a standard deviation of 25 games. He currently places orders for new games, which cost \$10 each, when the stock level drops to 80 games. If holding costs are 22 percent, how much will costs increase if Bill adopts a service-level policy of 99 percent during the reorder lead time?

**3-14** The annual demand for teak end tables at Salty Parker's Casual Furniture is 200 tables. Carrying cost for the table is \$50 per unit held per year, and the cost of placing an order is \$30. If the cost of maintaining a backorder per year is \$40, determine the optimal order quantity and planned backorder quantity for the tables.